

# MODELLING AND PARAMETRICAL APPROXIMATION OF AN ELECTRIC ARC FURNACE OF STEELMAKING

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**Abstract:** Electrical arc is a stochastic process; which is the principal cause of power quality problems, including voltages dips, harmonic distortion, unbalance loads and flicker. So it is difficult to make an appropriate model for an EAF. The factors that effect EAF operation are the melting or refining materials, melting stage, electrode position (arc length), electrode arm control and short circuit power of the feeder.

So arc voltages, current and power are defined as a nonlinear function of the arc length. In this article we propose our own empirical function of the EAF and model for the mean stages of the melting process. This study is important, because improvement of Electric Arc means high productivity (in tons/year) and lowest possible costs arising from energy consumption, electrode and refractory wear.

**Key words:** EAF, Electrical arc, Modelling, Power Quality, Steelmaking.

## 1. Introduction.

Nonlinear loads are the principal cause of power quality problems including voltage dips, harmonic distortion and flicker [2, 11, 12]. Electric arc furnace is the worst nonlinear loads type, and its nonlinearity is due to the chaotic nature of arc impedance [6], where its conductivity is determined from its temperature and pressure [10]. The increasing in iron demand, such as in vehicle industries, encourage the steel-works to invest more and more in the recovery of metals, thanks to electrical or chemical furnaces. The electric arc furnace is used to provide high quality steels from a raw material of steel scrap. Typical furnace is

shown in figure 1. It consists of a refractory lined shell and removable roof. Three graphite electrodes, held in clamps on the end of a supporting mast arm, pass through holes in the furnace roof. Electrical power is supplied to the electrodes by an adjustable voltage tap transformer, and the heat generated by electric arcs striking between the electrodes and the scrap melts. The maximum electrical power to heat conversion occurs for a particular length of electric arc [7], and any deviation from this optimum length impairs the power utilisation efficiency. The steel scrap surface is irregular by nature of the scrap, and, as parts of the scrap melt, it moves about, changing the contours of the surface. Thus, random disturbances in the arc length occur continuously. It is the function of the position control system to respond to such disturbances by moving the electrode to maintain the arc length at its preset value [8].

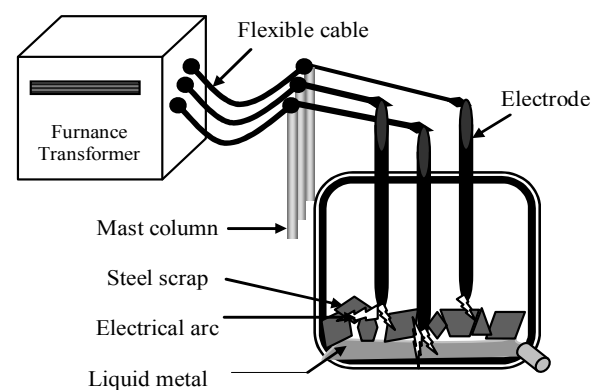


Fig.1 Typical electrical arc furnace

## 2. Typical EAF Process.

First we charge the furnace with scrap, after that the electrodes could be lowered, each of which has its own regulator and mechanical drive. The electrodes are connected to the furnace transformer's, which may be rated from 90 to 265 volts, thanks to 9 taps.

To achieve meltdown as quickly as possible one must follow the following stages [1, 3].

Stage-1: The current is initiated by lowering the electrodes, above the material.

Stage-2: Electrodes bore through the scrap to form a pool of liquid metal.

Stage-3: Electrical arc will be lengthened by increasing the voltage to maximum power.

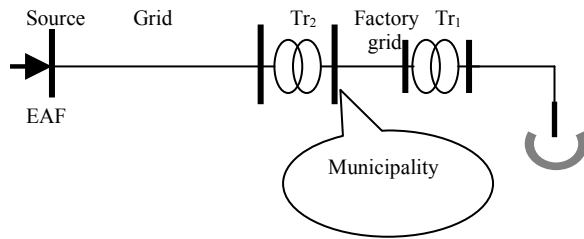
Stage-4: Arc length is changed so that the shorter arc will deliver a higher portion of its heat to the metal below the electrode.

Stage-5: Chemical treatments to improve steel quality is done under low power to maintain steel liquid

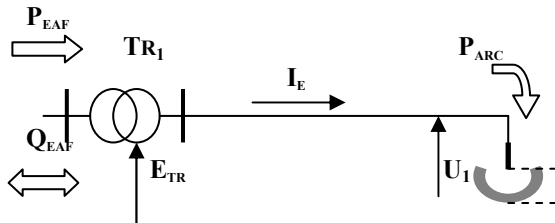
Stage-6: Stop of melting.

## 3. Model description

Our EAF melt steel, by applying an AC current to a steel scrap charge by means of graphite electrodes. It requires about 520 kwh/ton, and produce 700t/year approximately Fig 2, a.



a. EAF supply.



b. Measured parameters.

Fig.2. Studied mode.

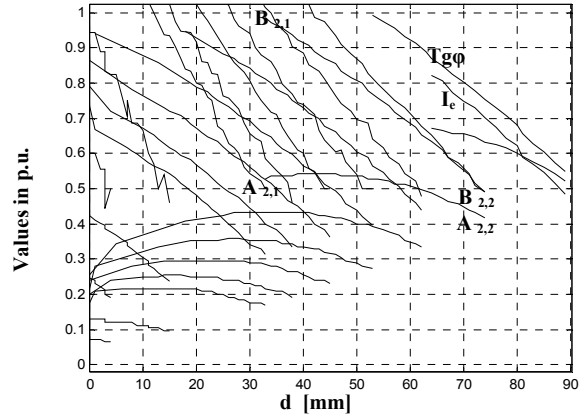


Fig.3. EAF process [2]

All the processes of electrical arc furnace (appendix A) can be summarized in figure 4 [9]. we have record 32 measurements of each measured parameter for 9 transformer taps Fig.3.b .normal operation must make the compromise between the limitations according to maximum power and acceptable current respectively  $[A_{n,1} \ A_{n,2}]$  and  $[B_{n,1} \ B_{n,2}]$ , where n is tap index. Then conferring itself to this constraint the adjustment law of electrodes position will be done according to  $S_{max}$

## 4. Treatment of measured parameters.

The EAF is modelled together with the neighbouring network [4]. The circuit equation of the furnace transformer to the end of electrodes can be written as follow

$$E_{tr} = \sqrt{3}Z_1 I_e + U_1 \quad (1)$$

Where  $U_1$ ,  $I_e$  &  $Z_1$  are respectively electrode voltage, current and impedance of EAF transformer with flexible cable

$$\text{Then, } Z_1 = \frac{[E_{tr} - U_1]}{\sqrt{3}I_e} = \frac{\Delta U_1}{\sqrt{3}I_e} \quad (2)$$

$$Z_1 = \sqrt{R_1^2 (I_2, T) + X_1^2 (T)} \quad (3)$$

$$R_1 = \frac{P_{EAF} - P_{arc}}{3I_e^2} \quad (4)$$

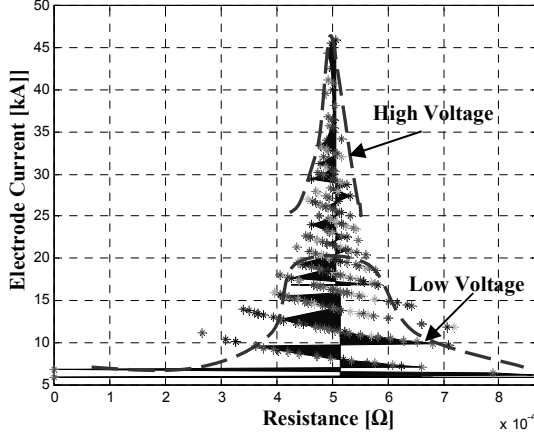
Where:

$P_{EAF}$  : is total active power of EAF.

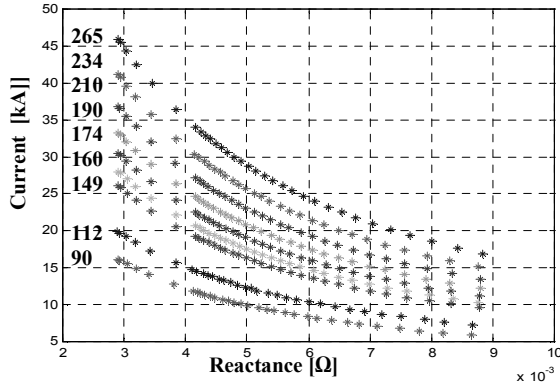
And  $P_{arc}$  : is the active power of arc.

So, from equations (1, 2, and 3) we can deduct.

$$X_1 = \frac{1}{\sqrt{3}I_e} \sqrt{\Delta U_1^2 - \frac{[P_{EAF} - P_{arc}]^2}{3I_e^2}} \quad (5)$$



a. Distribution of  $R_1$



b. Distribution of  $X_1$

Fig.4. Calculation of  $Z_1$  form the 9x32 measurements

On figure 4 a & b we show the variation of resistance  $R_1$  and reactance  $X_1$  of the transformer with the flexible cable which supplies the electrodes.

$$R_1 = R_{tr} + R_{\text{flexible cable}} \quad (6)$$

Indeed for the various tests carried out:

- $R_1$  has a Gaussian distribution; this is due to the combined effect of the current and the time of its application. Dispersion has a more important in low voltage, because metal takes more time to melt; from where it overheating the transformer winding and flexible cable.

- As reactance  $X_1$  is the consequence of electromagnetic fields, which weakened with the increase of temperature, gives it a deadened exponential variation.

The variation of  $R_1$  “Fig.4.a” is the consequence of the fast growing temperature defined as a temperature coefficient caused by the important current supplied during the melting process. In order to reduce this parametric dispersion we propose reinforcement in cooling by forced ventilation of transformer windings and increase water flow which crosses the flexible cables.

$$R_{arc} = \frac{P_{arc}}{3I_e^2} \quad (7)$$

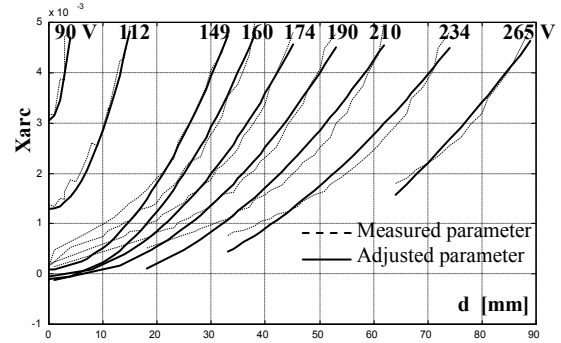
$$Q_{EAF} = Q_{arc} + \Delta Q \quad (8)$$

$$Q_{arc} = Q_{EAF} - 3I_e^2 X_1 \quad (9)$$

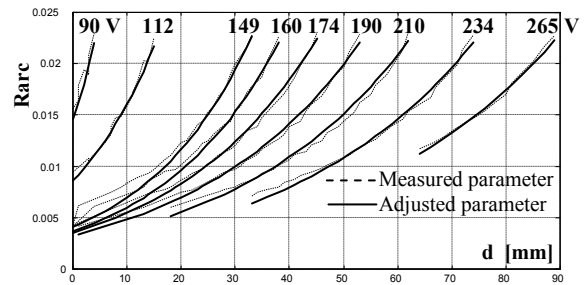
Where  $Q_{EAF}$  is total reactive power of EAF.

And  $Q_{arc}$  is the reactive power of arc.

$$X_{arc} = \frac{Q_{arc}}{3I_e^2} \quad (10)$$



a. Variation of  $X_{arc}$



b. Variation of  $R_{arc}$

Fig.5. Variation of electric arc impedance.

On figures 5a&b we show the variation of  $R_{arc}$  and  $X_{arc}$  with the distance between electrodes and scrap “d”.

The continuous line represents measured parameter, and the discontinuous line represents adjusted parameter when the adjustment law of electrodes position will be done according to  $S_{\max}$ . Following to this treatment an empirical model is proposed:

$R_{arc} = A_R(u)e^{\alpha(u)d}$ ; Where

$$A_R = \frac{[0,7.(U-210)^2 + 1,7]}{50^2} \cdot 10^{-3};$$

$$\alpha = 0,097e^{0,011(90-U)} - \frac{1,7}{(U-112)^2 + 80} + \frac{100}{(U-360)^2 + 50}$$

$X_{arc} = A_X(u)d^2 + B_X(u)$ ; Where

$$A_X = 1,05 \cdot 10^{-3} e^{0,075(90-U)};$$

$$B_X = \frac{3,14}{153} - 3 \cdot 10^{-3} e^{0,075(90-U)}$$

$d$ : Is the distance between electrode and scrap.

In the operating zone the arc impedance decreases with the increase of voltage and increases with the distance between electrodes and metal, "Fig.6, 7". The analysis of the results shows that for high voltages and short distance of arc, the electrostatic field created between the electrode and metal is more important as the electromagnetic fields, thus gives to the arc a capacitive character. Can be observed in figure 5 by the negative values of  $X_{arc}$ .

For this purpose we give a model of electric arc shown in figure 6.

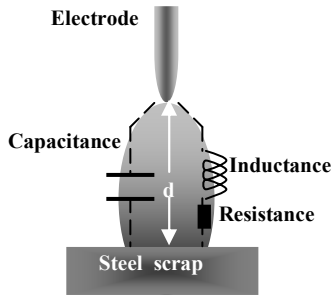


Fig.6. Electric arc model.

$$Q_{arc} = Q_{arc}^L + Q_{arc}^C \quad (11)$$

$$Q_{arc}^L = K_L d \quad (12)$$

$$Q_{arc}^C = -K_C / d \quad (13)$$

$Q_{EAF}^L$ : Is the inductive reactive power of arc.

$Q_{arc}^C$ : Is the capacitive reactive power of arc.

From equations (11, 12, 13) we can writ

$$Q_{arc} = \frac{[K_L d^2 - K_C]}{d} \quad (14)$$

$$K_L(n) = \frac{Q_{arc}(n+1)d(n+1) - Q_{arc}(n)d(n)}{d^2(n+1) - d^2(n)}$$

$n$  is the measurement number

$$K_C(n) = K_L(n)d^2(n+1) - Q_{arc}(n+1)d(n+1)$$

$$Q_{arc}^L = K_L d = 3X_{arc}^L I_e^2 \Rightarrow$$

$$X_{arc}^L = K_L d / 3I_e^2 \quad (15)$$

$$Q_{arc}^C = -K_C / d = -U_1^2 / X_{arc}^C \Rightarrow$$

$$X_{arc}^C = U_1^2 d / K_C \quad (16)$$

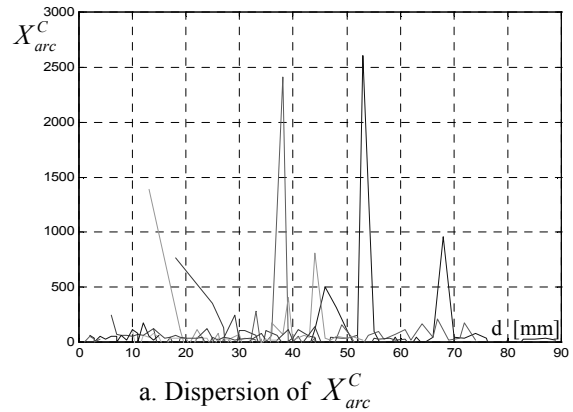
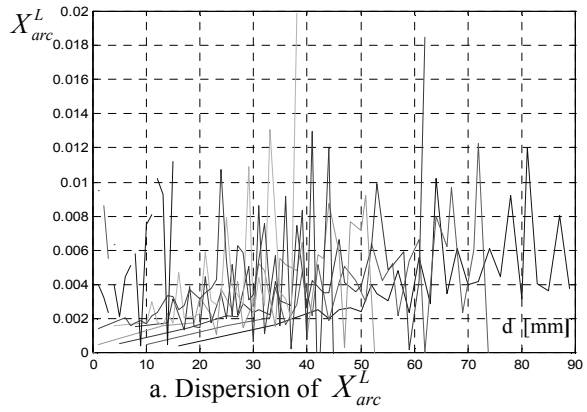


Fig.7. Calculation of  $Z_{arc}$  form the 9x32 measurements

After numerical treatment of measured parameters we propose a model for the principal stages of melting process summarised in figure 8.

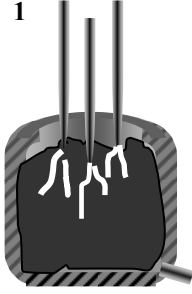
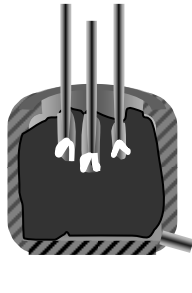
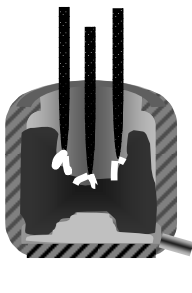
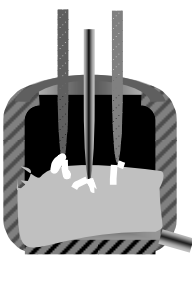
Stage	Model
1	High voltage long arc 
2	High voltage short arc 
3	Medium voltage short arc 
4	Low voltage short arc 

Fig.8.The proposed model of EAF for each melting stage

The major part of power quality problems occurs in the stage 1 & 2, because of the physical movement and settling of the scrap.

Irregularity in the voltage wave forms is caused by abrupt initiation [5] and interruption of current witch provides a source of harmonic currents “Fig 9a&b”. Thus voltage and current waves deviate considerably from symmetrical sinusoidal form.

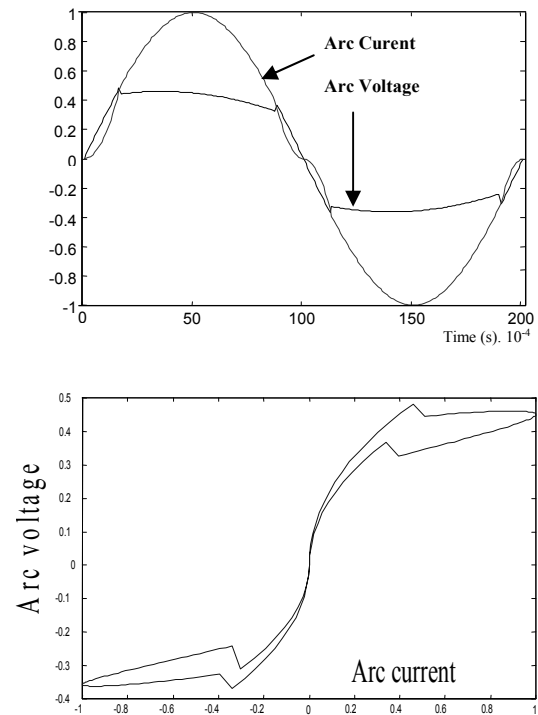


Fig.9. Temporal and [IV] representation of electric arc current & voltage [5].

We show in figure 9 clearly a nonlinear load in EAF operation when the voltage supply and the current are not the same shape and that gives the birth of the harmonic.

So we propose to substitute the electrical energy by a chemical one, like natural Gas, and the EAF will be electrically supplied only in stage 3 & 4.

Because in the stage 3 the electrical arc is lengthened by increasing the voltage, so the current became very chaotic and no linear. But in the stage 4 the arc length is, in this case the voltage will be inflected.

## 5. Conclusion

This analysis leads to the conclusion that the arc behaves in such a way that all the arc characteristics are controlled by the expansion of the arc, which is the main feature used to physically describe the arc

behaviour. The arc expansion is evident from the arc shape, which is defined as the region where conduction of electricity takes place. The arc shape depends on: current density, magnetic flux density, electric conductivity, electric potential, and temperature fields.

The proposed model reveals a new parameter of the electrical arc furnace which is the capacitances. Because of The continuous adjustment of electrode position, the integration of this model in the regulation loop, reduce the operator action; thus reduction of human errors due to the visual estimate, then this automation enables us to make a better management of energy from where the reduction of the consumption (kWh/tonne).

The empirical relations of the condenser and the inductance of the furnace, enable us to avoid some very dangerous oscillations of the current and the voltage which disturb the nearness loads. Our recommendation to steel makers is to substitute electrical energy for stage 1 & 2 by a chemical one, because of power quality constraint.

#### Annex A:

##### EAF characteristics

Transformer rating:	12, 5 [MVA]
Short circuit reactance:	2, 9 [mΩ]
Maximum electrode current	30, 84 [kA]
Number of voltage taps:	9
Voltage range:	[90 V ÷ 265 V]
Primary voltage:	63 [kV]
Weight capacity:	80 t
Temperature gradient:	3 ÷ 4 °C/mn
Furnace diameter:	2, 47 [m]
Electrode diameter:	0, 35 [m]
Distance electrode to wall:	0, 7 [m]

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