

Control of the Three Phase four-wire four-leg SAPF Using 3D-SVM Based on the Two Methods of Reference Signals Generating CV and SRF in the dqo-axes

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Abstract: In this paper, the performance of the two algorithms of generating reference signals for three phase four-wire four-leg SAPF are compared in load conditions balance and unbalance. The algorithms that are used for this study are the synchronous reference frame theory (SRF) and cross-vector theory (CV), in the dqo-axes, and the voltage and current regulation is performed by the PI type controller, using the 3D-SVM technique to generate the switching signals, It is shown by simulation studies of the source current harmonics, the switching loss of the converter is reduced to the reference method with synchronous using 3D-SVM technical, Simulation results show the superiority of synchronous reference frame theory both in definition and compensation.

Keywords: Three phase four-wire four-legs SAPF, 3D-SVM, Zero sequence, PI, CV, SRF, dqo-axes.

1. introduction

Le Distribution networks are faced with new challenges and new opportunities of an electrical system in full technological developments. From the technical viewpoint, the main change concerns the nature of network connected loads; firstly, conventional passive load have undergone a very important development, and secondly, new active loads have been connected to the network [1]. These new charges generate major disturbances in the power network such as voltage disturbances caused by the passage of perturbation currents as harmonic currents, reactive and unbalanced.

The technical of reducing harmonic currents, by passive LC filters [5], [7], [10], is generally formed by capacitors and inductors connected to the network. Each harmonic (5th, 7th, 11th, 13th) requires its own passive filter. This means that the filter can not be designed in general case, but must be designed according to each application. This solution has the advantages of simplicity and low cost. However, among the disadvantages are: designed for a specific application, the size and positioning of the filter elements, the risk of resonance problems.

The active power filters are a new solution for the compensation of harmonic pollution in power systems. We can distinguish two types of active filters, series and shunt. The shunt active power filter makes the compensation of harmonic currents and reactive power [2]. The analysis of the operation of a three-leg active filter connected to a four-wire network shows that it cannot compensate for perturbations due to single-phase non-linear loads connected to a four-wire network. Harmonic currents circulating in the network remain partly compensated and amplitude of the zero sequence current is not reduced, to remedy it will be necessary to provide a four-leg shunt active filter [3]-[14].

Among the various topologies the three phase four-wire four-leg SAPF based on voltage source inverter is the most common one because of its good efficiency. Its performance depends on the adoptive control approaches. There are four major parts of an active power filter controller. The first is the reference signal generation technique, the second is that switching signals

Equation (4) so becomes:

$$\begin{bmatrix} i_{fo}^* \\ i_{f\alpha}^* \\ i_{f\beta}^* \end{bmatrix} = A' \begin{bmatrix} v_{lo} & 0 & v_{l\beta} & v_{l\alpha} \\ v_{l\alpha} & -v_{l\beta} & 0 & v_{lo} \\ v_{l\beta} & v_{l\alpha} & -v_{lo} & 0 \end{bmatrix} \begin{bmatrix} p_f^* \\ q_{fo}^* \\ q_{f\alpha}^* \\ q_{f\beta}^* \end{bmatrix} \quad (5)$$

The inverse Concordia transform calculates the reference currents in the abc -axes as follows:

$$\begin{bmatrix} i_{f1}^* \\ i_{f2}^* \\ i_{f3}^* \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & 0 & \frac{1}{\sqrt{2}} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} & \frac{1}{\sqrt{2}} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} & \frac{1}{\sqrt{2}} \end{bmatrix} \begin{bmatrix} i_{f\alpha}^* \\ i_{f\beta}^* \\ i_{fo}^* \end{bmatrix} \quad (6)$$

The Fig.2 shows the diagram of the cross vector method.

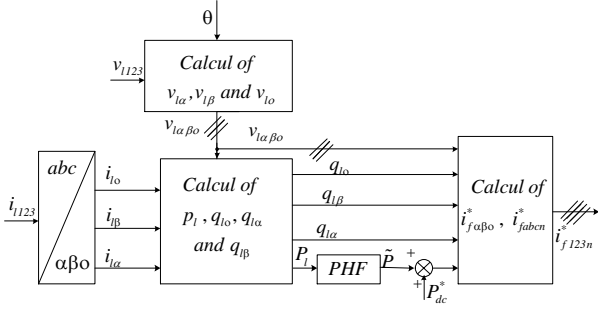


Fig. 2 Schematic diagram of the cross-vector theory

3.2 Synchronous Reference Frame Theory (SRF)

The SRF theory gave very good results for the compensation of three phase three wire electricity network. For three phase four wire electricity networks, a theory based on the modification of the cross-vector theory of dqo -axes, has been proposed [20].

Fig. 4 shows the basic principle of this SRF theory applied to a three phase four wire four-leg SAPF [21].

The SRF theory firstly requires the transformation of the three-phase load currents in the $\alpha\beta$ -axes as follows:

$$\begin{bmatrix} i_{l\alpha} \\ i_{l\beta} \\ i_{lo} \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix} \begin{bmatrix} i_{l1} \\ i_{l2} \\ i_{l3} \end{bmatrix} \quad (7)$$

We obtain in dqo -axes the following currents:

$$\begin{bmatrix} i_{ld} \\ i_{lqo} \\ i_{lq\alpha} \\ i_{lq\beta} \end{bmatrix} = \begin{bmatrix} 0 & \sin(\theta) & -\cos(\theta) \\ 0 & \cos(\theta) & \sin(\theta) \\ -\cos(\theta) & 0 & 0 \\ -\sin(\theta) & 0 & 0 \end{bmatrix}^{-1} \begin{bmatrix} i_{lo} \\ i_{l\alpha} \\ i_{l\beta} \end{bmatrix} \quad (8)$$

The signals $\sin(\theta)$ and $\cos(\theta)$ related to the mains voltage,

The currents i_{chd} and i_{chq} can be expressed as the sum of two components, a continuous and another alternative, such as:

$$\begin{bmatrix} i_{ld} \\ i_{lq} \end{bmatrix} = \begin{bmatrix} \bar{i}_{ld} & \tilde{i}_{ld} \\ \bar{i}_{lq} & \tilde{i}_{lq} \end{bmatrix} \quad (9)$$

With \bar{i}_{chd} , \bar{i}_{chq} are the direct components of i_{chd} and i_{chq} , and \tilde{i}_{chd} , \tilde{i}_{chq} alternative components of i_{chd} and i_{chq} respectively.

The filter reference currents are expressed in dqo -axes by:

$$\begin{bmatrix} i_{ld}^* \\ i_{lq}^* \\ i_{f\alpha}^* \\ i_{f\beta}^* \end{bmatrix} = \begin{bmatrix} 0 & 0 & -\cos(\hat{\theta}) & -\sin(\hat{\theta}) \\ \sin(\hat{\theta}) & \cos(\hat{\theta}) & 0 & 0 \\ -\cos(\hat{\theta}) & \sin(\hat{\theta}) & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{fd}^* \\ i_{fq}^* \\ i_{f\alpha}^* \\ i_{f\beta}^* \end{bmatrix} \quad (10)$$

$$\text{With: } \begin{bmatrix} i_{fd}^* \\ i_{fq}^* \\ i_{f\alpha}^* \\ i_{f\beta}^* \end{bmatrix} = \begin{bmatrix} i_{ld} \\ i_{lq} \\ i_{lq\alpha} \\ i_{lq\beta} \end{bmatrix}$$

The inverse Concordia transform calculates the reference currents in the abc -axes as follows:

$$\begin{bmatrix} i_{f1}^* \\ i_{f2}^* \\ i_{f3}^* \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & 0 & \frac{1}{\sqrt{2}} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} & \frac{1}{\sqrt{2}} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} & \frac{1}{\sqrt{2}} \end{bmatrix} \begin{bmatrix} i_{f\alpha}^* \\ i_{f\beta}^* \\ i_{fo}^* \end{bmatrix} \quad (11)$$

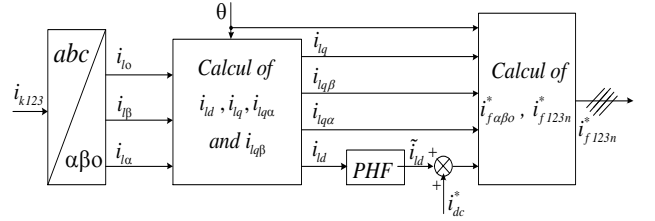


Fig. 3 Schematic diagram of the Synchronous Reference Frame theory

4. Technique for generating switching signals

The objective of control is to generate the opening and closing commands of the switches, so that current is injected by the inverter currents nearest reference.

4.1 Three Dimensional Space Vector Modulation with Null Vector

The major advantage of a four-leg inverter is that the DC bus utilization can be improved by using 3D Space

Vector Modulation [8]-[9].

4.2 Prism identification

Six prisms in the 3D space can be identified and numbered as Prisms I through VI (Fig. 3). Within the selected prism, there are six non-zero switching state vectors and two zero switching state vectors. Fig. 4 shows the physical positions of the switching state vectors in $\alpha\beta o$ -axes [10]-[13].

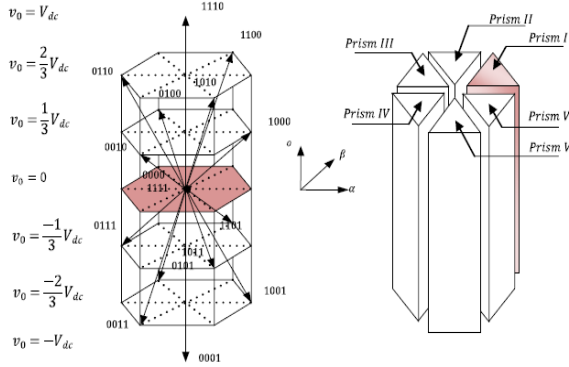


Fig. 4 Voltage vectors in abc system in the $\alpha\beta o$ -axes, and the selection of prism.

4.3 Tetrahedron identification

The tetrahedron is formed by three non-zero voltage vectors and two other zero vectors, as shown in Fig. 5. Fig. 6 describes the representation of tetrahedron 1 plans belonging to prism I [10]-[11].

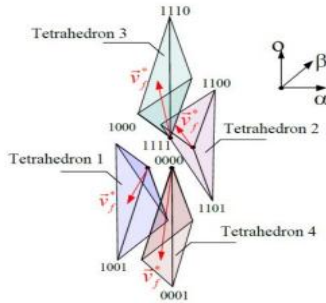


Fig. 5 Representation of tetrahedra in the prism I

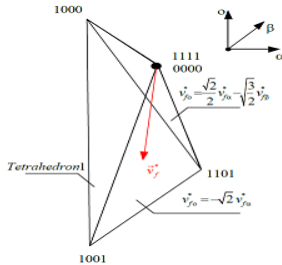


Fig. 6 Projection of the reference vector on the adjacent vectors

4.4 Duty Cycle Calculation

For the tetrahedron i of the prism j , the states vectors of the inverter (v_x, v_y, v_z, v_0) are the adjacent vectors to the reference voltage vector. These vectors are applied individually for certain periods t_x, t_y, t_z and t_0 , such that

$$\bar{v}^* \text{ is equal to the mean value of those vectors for a period of switching: [12]}$$

$$\bar{v}^* = \bar{V}_x + \bar{V}_y + \bar{V}_z + \bar{V}_0 \quad (12)$$

With: $x, y, z \in \{2, \dots, 15\}$ and $o \in [1, 6]$.

The mean reference vector is expressed by:

$$\bar{v}^* = \frac{1}{T_h} \int_t^{t+T_h} \vec{v} dt \quad (13)$$

As the period of switching is very small, the mean voltage value can be considered as constant; and as the vectors V_x, V_y, V_z et V_0 are fixed, it follows that:

$$\bar{V}_i = \frac{1}{T_h} \int_t^{t+t_i} V_i dt = \frac{1}{T_h} V_i t_i \quad (14)$$

With $i=x, y, z, 0$.

Then

$$T_h \bar{v}^* = t_x V_x + t_y V_y + t_z V_z + t_0 V_0 \quad (15)$$

$$t_0 = T_h - t_x - t_y - t_z \quad (16)$$

4.5 The Control Pulses Generation

The fig. 7 shows, on a switching period, the distribution of voltage vectors to be applied in the first prism tetrahedron [9].

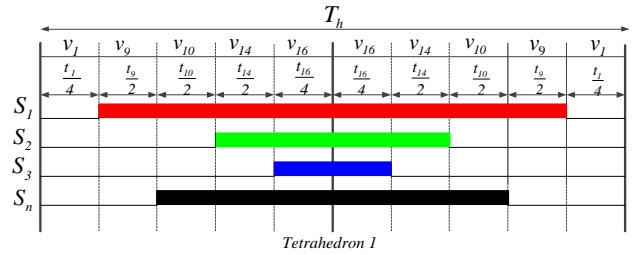


Fig. 7 Principle of generation in the pulses by 3D-SVM

5. Simulation results and discussion

The simulations were performed considering a three-phase four-wire four-leg SAPF feeding three unbalanced nonlinear loads, as shown in fig. 1. The parameters of SAPF are shown in Table 1.

The simulation of the three phases four-wire four-leg SAPF was carried out under the following conditions:

- The switching frequency: $f_s = 14$ kHz.
- The reference voltage: $V_{dc \text{ ref}} = 800$ V.

Table 1: System parameters for simulation and load specifications

| | |
|---------------------------------|-------------------------|
| Capacitance of the capacitor | 5 mF |
| Coupling impedance R_f, L_f | 0.1 m Ω , 0.1 mH |
| The source voltage and frequenc | 220 V, 50Hz |
| Source impedance R_s, L_s | 1 m Ω , 1 mH |
| Line impedance R_{ch}, L_{ch} | 1 m Ω , 1 mH |
| Load impedance R_l, L_l | 5 Ω , 10 mH |

5.1 Simulation du système avant le filtrage

The simulation results of the system before compensation are given in fig. 8.

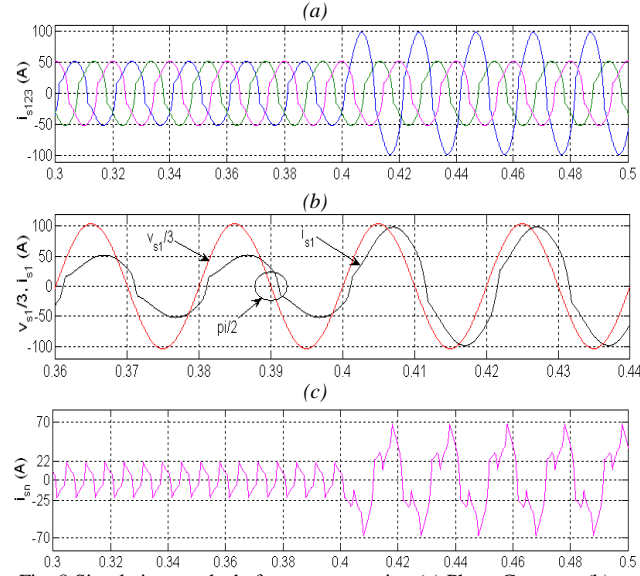


Fig. 8 Simulation results before compensation (a) Phase Currents, (b) Voltage and current source of the first phase, (c) Neutral Current

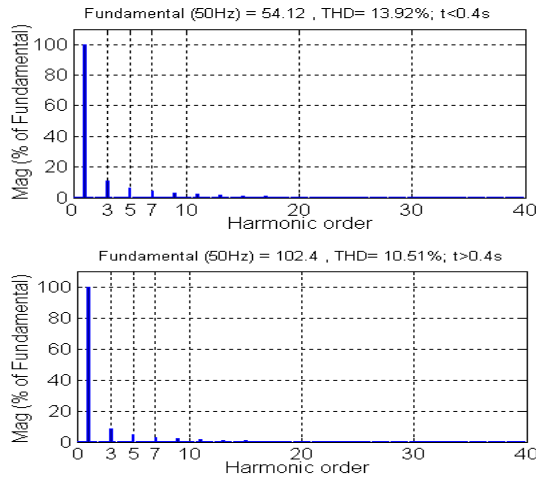


Fig. 9 %THD load current before compensation

The fig. (8-a) shows the current waveform of the load, it is a highly non-sinusoidal current and deformed and there is not in sync with the corresponding voltages (power factor is $F_p = 0$). The fig. (8-c) shows the shape

of neutral current with a maximum value of 22A in the balanced case and 70A in the unbalanced case. Fig. (9-a,b) shows the first phase source current's THD. Before unbalanced load ($t < 0.4s$), the total harmonic distortion (THD) is 13.92%, when after ($t > 0.4s$) it's 10.51%.

5.2 Simulation with The cross-vector theory

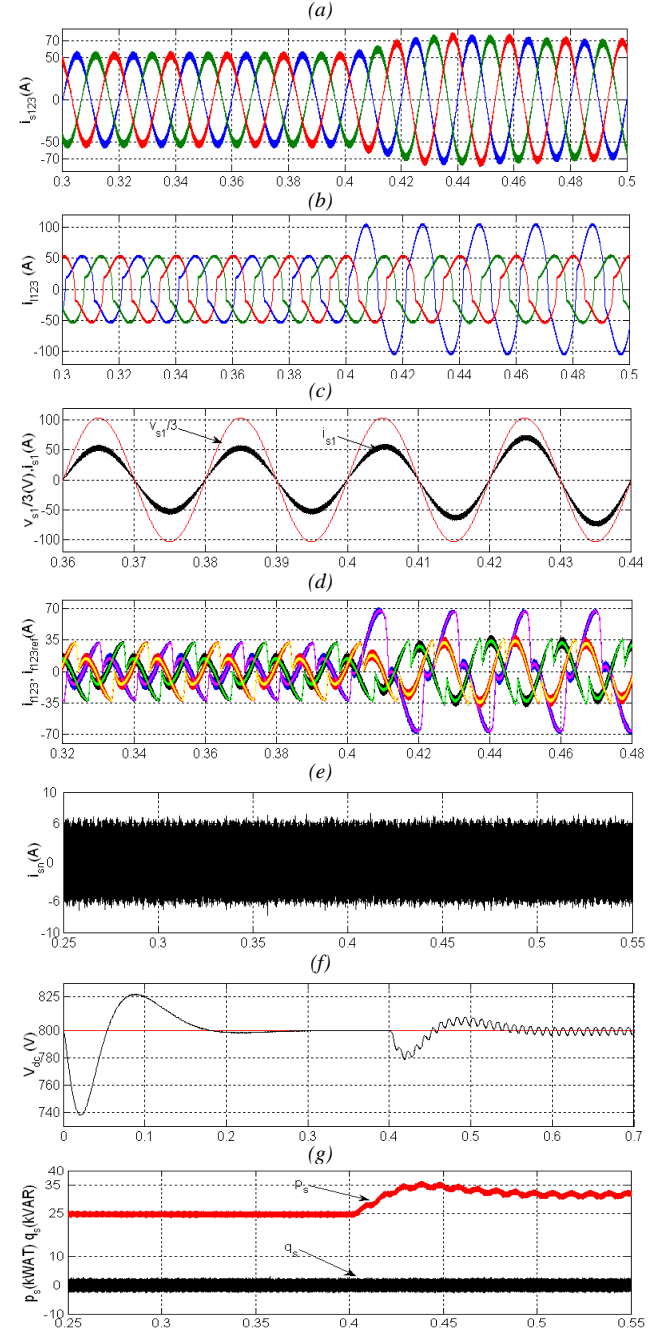


Fig.10 The cross-vector theory simulation results: (a) source currents after compensation (b) load current after compensation (c) Voltage and current source of the first phase after filtering (d) Injected currents by

the active filter (e) Neutral current after filtering, (f) DC link voltage, (g) Real and imaginary powers.

5.3 Simulation with The SRF theory

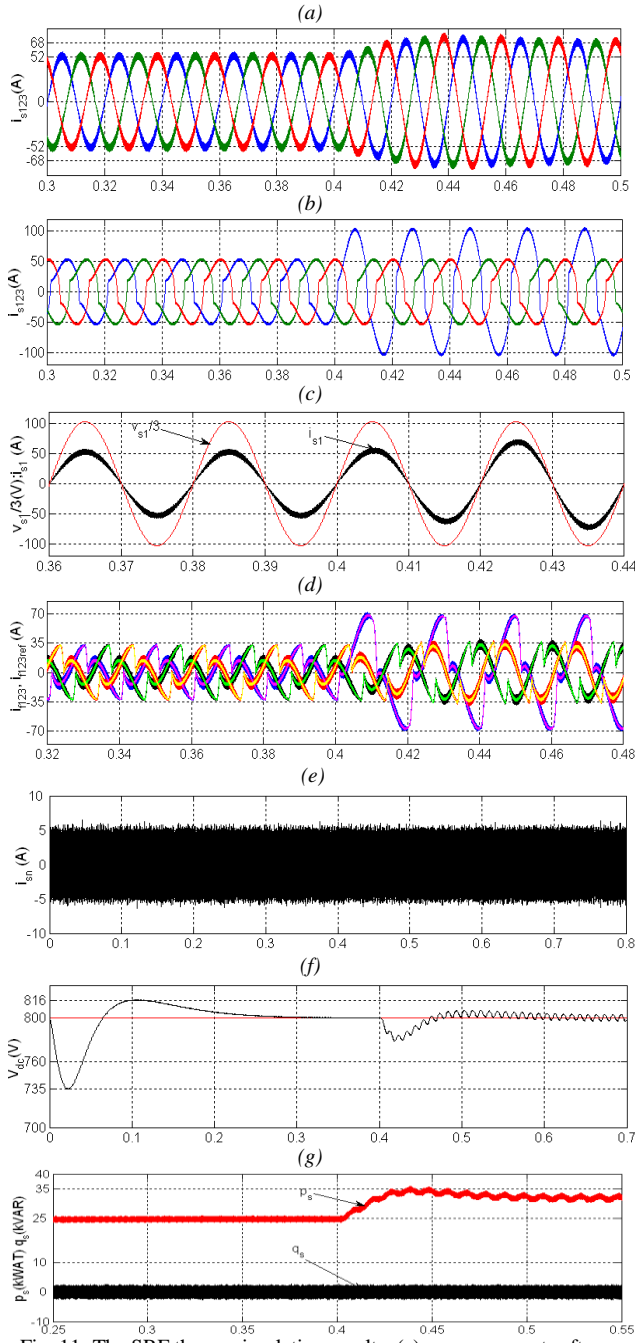


Fig. 11 The SRF theory simulation results: (a) source currents after compensation (b) load current after compensation (c) Voltage and current source of the first phase after filtering (d) Injected currents by the active filter (e) Neutral current after filtering, (f) DC link voltage, (g) Real and imaginary powers.

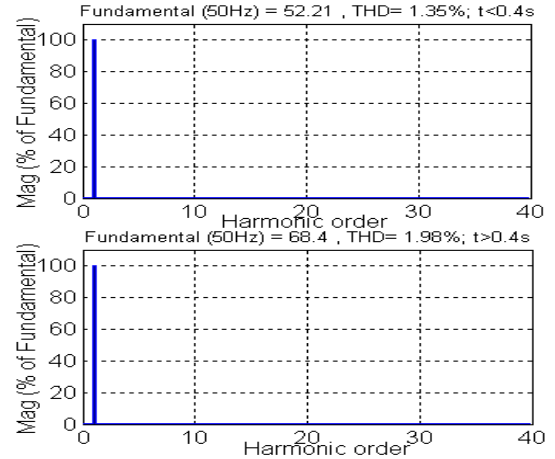


Fig. 12 %THD source current before and after unbalanced load with the cross-vector theory

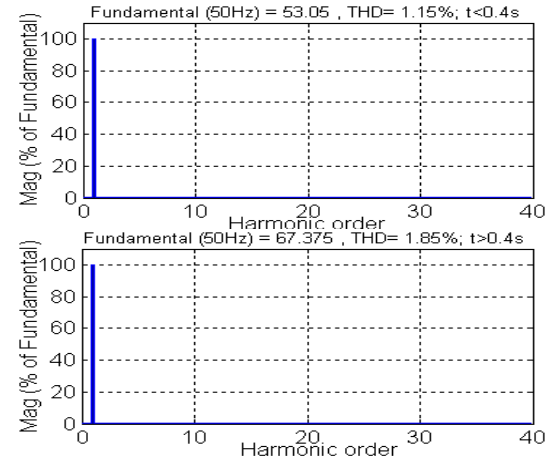


Fig. 13 %THD source current before and after unbalanced load with the SRF theory

The figs. (10.11-a) shows the source current waveform after filtering is sinusoidal. The figs. (10.11-b) represent the load current form, it is non-sinusoidal current and highly deformed. It is noted that the current network is still in phase with the corresponding voltage, and the power factor is unitary as shown in figs. (10.11-c). The figs. (10.11-d) represents the active filter injected currents. The figs. (10.11-e) show that after compensation the neutral current is in the range of ± 6 A with CV theory and the range of ± 5 A with SRF theory. The capacitor voltage is stabilized at its reference value with a small static error as shown in figs (10.11-f). Figs (10.11-g) show the real and imaginary power of source. It can be seen here that the active power p_s is delivered almost constantly by the source although the loads demand a fluctuated active power.

Observing the reactive power q_s waveform, the source is successfully forced not to supply the reactive power as the value of q is always around 0. Figs. (12-13) show the first phase source current's THD for the two theories.

Before unbalanced load ($t < 0.4s$), the total harmonic distortion (THD) is 1.35% for the CV theory and 1.15% for the SRF theory, when after ($t > 0.4s$) it's 1.98% for the CV theory and 1.85% for the SRF theory.

6. Conclusion

For industrial equipment and consumer products, improving the quality of energy is a prerequisite. The SAPF offers better performance than other methods of compensation. the structure of the three phase four-wire four-leg Shunt Active Power Filter allowing compensation of harmonic currents in the network, reducing the amplitude of the zero sequence current and improve the power factor.

The results from the simulation of two algorithms of control, we showed that these two algorithms can compensate for harmonic currents in the network and reducing the magnitude of the zero sequence current, The two algorithms, performed into *dqo*-axes, was implemented using 3D SVM. However, we demonstrate that the algorithm (SRF) is better because it reduces the rate THD network side.

The table 2 gives the THD and amplitude of the neutral current comparison of 3D-SVM control technique with CV and SRF control strategy using Matlab/Simulink.

Table 2: Comparison of the different techniques

| | CV | | SRF | |
|--|---------------|-----------------|---------------|-----------------|
| | Balanced Load | Unbalanced Load | Balanced Load | Unbalanced Load |
| Source current THD % | 1.35% | 1.98% | 1.15% | 1.85% |
| The amplitude of the neutral current (A) | 6 A | | 5 A | |

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