# Optimal Reactive Power Dispatch Using Self-Balanced Differential Evolution Algorithm

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Abstract—Reactive Power Dispatch (RPD) is one of the major optimization problems in power system which has multi-variable and nonlinear characteristic with equality and inequality constraints. Differential Evolution (DE) algorithm is a simple but powerful algorithm widely used to solve power system optimization problems. In this paper a new and novel variant called Self-Balanced Differential Evolution (SBDE) is developed to improve the performance of DE algorithm and balance the exploration and exploitation processes. Two different objective functions have been considered viz., the minimization of total real power loss and total bus voltage deviation under normal and stressed conditions. Voltage magnitude of the generator, transformer tap ratio and reactive power of capacitor banks are considered as control variables. The proposed approach is applied in IEEE 57-bus and IEEE 118-bus test systems for performance assessment. The obtained results demonstrate the proficiency of the proposed approach and the results are compared with the results reported in the literature.

Keywords — Power System, Evolutionary Computing, Optimization, Self-Balanced Differential Evolution, Reactive Power Dispatch.

#### INTRODUCTION

Optimal operation and planning of power system networks have been an economic criterion. Optimal Power Flow (OPF) is a powerful concept for power system planning and operation first formulated by Carpentier in 1960s. Optimal Reactive Power Dispatch (ORPD) is a sub problem of OPF. It is a procedure that allocates the reactive power generation so as to minimize the transmission loss, results in lowest production cost satisfying the operation constraints [1].

ORPD has significant influence on the economic and secure operation of power systems. It is an important tool both in planning for the future and day to day operation of power system. ORPD is a mixed integer problem which has both continuous and discrete variables. Earlier it has been solved by conventional optimization approach such as linear programming, interior point method [2] and quadratic programming [3]. Due to the multi-modal

characteristics and the non-linearity, non-differential, nonconvex nature of the ORPD problem, the majority of the conventional optimization techniques may converge to a local optimum [4]. To overcome the drawbacks in conventional approach, recently heuristic algorithms like Genetic Algorithm (GA) [5], Particle Swarm Optimization (PSO) [6], Ant Colony Optimization(ACO) [7], Differential Evolution (DE) [8], Evolutionary programming (EP) [9], Seeker Optimization [17], Gravitational search algorithms (GSA) [15], and Opposition based Gravitational search algorithms (OSGA) [16] are used to solve ORPD problem. Differential Evolution algorithm is simple but powerful and efficient evolutionary algorithm in solving global optimization problems proposed by Storn and Price [4] in 1995. The good performance of DE in terms of convergence speed, accuracy, and robustness makes it attractive for applications to various real world optimization problems. Simple DE has been used to solve the reactive power optimization problem in [8], where the value of mutation factor (F) and Crossover Ratio (CR) is assumed constant for all generation and makes unsuitable for all system. D.Devaraj et al. [18] have proposed GA based ORPD for voltage stability enhancement in which they consider a fixed value for crossover ratio.

DE with small modification is also applied to solve ORPD problem [13]. Though DE is a simple algorithm, but different control parameters settings show different characteristics. A larger value of F is effective for global search, whereas smaller can accelerate the convergence characteristics. On the other hand, a larger CR results in higher diversity of the population, since the trial vector will inherit more information from the mutant vector. However, a smaller CR focuses on local exploitation since the target vector will contribute more information to the trial vector. Indeed, it is still an issue to choose suitable settings of F and CR to balance the exploration and exploitation of DE during the evolution [11].

During the past years, many variants have been introduced in DE. Recently Harish Sharma et al. [11] have proposed a Self-Balanced Differential Evolutionary algorithm (SBDE). InDE mutation performs exploration (ability to expand the search space) and selection performs

exploitation (ability to find the optima around a good solution). To maintain the balance between exploration and exploitation a new control parameter called cognitive learning factor is introduced in DE. In this paper cognitive learning factor is denoted as 'C'. Mutation factor is also dynamically varied according to the earlier information. So these modifications improve the performance.

This paper proposes a novel SBDE algorithm to solve the ORPD problem. The problem is formulated as a nonlinear optimization problem with equality and inequality constraints. Two different objectives are considered such as minimization of real power loss and total voltage deviation under normal and stressed condition. The proposed algorithm is successfully tested on IEEE 57 and IEEE 118 bus systems and the simulation results are compared to those reported in the literatures.

The remainder of the paper is organized as follows: Section 2 presents the formulation of ORPD problem. Section 3 briefly explains the overview of DE. In Section 4 the algorithm of SBDE in solving the ORPD problem is presented. To analyze the performance of the SBDE algorithm, it is tested on IEEE 57, and IEEE 118 bus systems and the results are discussed in Section 5. Finally conclusions are drawn in the last section.

#### II. Problem Formulation

RPD problem is formulated as mixed integer problem with both continuous and discrete variables. The objective function of the RPD problem is expressed as follows.

#### 2.1 Objective functions

#### P<sub>loss</sub>: Minimization of real power loss

Minimization of real power loss is considered asthe one of the objective functions and is expressed in eqn.

$$Min f = \sum_{k=1}^{nl} P_{loss} = \sum_{i=1}^{NB} \sum_{j=1}^{NB} g_k (V_i^2 + V_j^2 - 2V_i V_j \cos(\delta_i - \delta_j))$$

(1)

 $g_k$ - Conductance of the k<sup>th</sup> line

 $v_i, v_i$  - Voltage magnitude at the end buses i and j of the kth line.

 $\delta$  - Voltage phase angle at the end buses i and j.

nl -number of transmission of lines

NB- total number of buses

### TVD: Minimization of total voltage deviation

Bus voltage is the most important thing when security and service quality indices are considered. To improve voltage profile, the load bus voltage can be minimized. The objective function total voltage deviation can be expressed as in eqn. (2).

Total Voltage Deviation 
$$= \sum\nolimits_{i=1}^{NPQ} |V_{Li} - V_{L}^{ref}| \quad (2)$$

Voltage at ithload bus.  $V_L^{ref}$  – 1 p.u.

NPQ - Number of load buses

#### 2.2 Equality constraints

These constraints eqns. (3) and (4) represent power balance equation

$$P_{Gi} - P_{Di} = V_i \sum_{j=1}^{NB} V_i \left( g_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \right)$$
 (3)

$$Q_{Gi} - Q_{Di} = V_i \sum_{i=1}^{NB} V_i \left( G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \right) \tag{4}$$

 $P_{Gi}$  – Real power generation of generator i.

 $Q_{Gi}$  – Reactive power generation of generator i.

 $P_{Di}$  – Real power demand at generator bus i

O<sub>Di</sub> – Reactive power demand at generator bus i

 $V_i, V_j$ - Voltage magnitude at bus i, j

NB- total number of buses

#### 2.3 Inequality constraints

Limits of the state and control variables are the inequality constraints expressed from eqn. (5) to (8).

$$V_{G_i}^{\min} \le V_{G_i} \le V_{G_i}^{\max}, i = 1, ..., N_G$$
 (5)

$$\begin{split} V_{G_{i}}^{\min} &\leq V_{G_{i}} \leq V_{G_{i}}^{\max}, & i = 1, ..., N_{G} \\ P_{G_{i}}^{\min} &\leq P_{G_{i}} \leq P_{G_{i}}^{\max}, & i = 1, ..., N_{G} \end{split} \tag{5}$$

$$Q_{C_i}^{min} \le Q_{C_i} \le Q_{C_i}^{max}, i = 1, ..., N_C$$
 (7)

$$T_i^{\min} \le T_i \le T_i^{\max}, i = 1, ..., N_T$$
 (8)

 $T_i^{\min} \leq T_i \leq T_i^{\max}, \ i = 1, ..., N_T$  (8)  $V_{G_i}^{\min}, V_{G_i}^{\max}$  - minimum and maximum limits of voltage at ith generator

 $P_{G_i}^{min}$  ,  $P_{G_i}^{max}$  - minimum and maximum limits of real power at ith generator

 $Q_{C_i}^{min}$ ,  $Q_{C_i}^{max}$  - minimum and maximum limits of capacitor banks

T<sub>i</sub><sup>min</sup>, T<sub>i</sub><sup>max</sup> - minimum and maximum limits of transformer tap settings

The reactive power generation Q<sub>G</sub>,loadbus voltage magnitude V<sub>L</sub> and line flow S<sub>L</sub> operating constraints are expressed in eqns. (9)

$$0_{G_i}^{\min} \le 0_{G_i} \le 0_{G_i}^{\max}, i = 1, ..., N_G$$
 (9)

$$\begin{aligned} &Q_{G_{i}}^{\min} \leq Q_{G_{i}} \leq Q_{G_{i}}^{\max}, & i = 1, ..., N_{G} \\ &V_{L_{i}}^{\min} \leq V_{L_{i}} \leq V_{L_{i}}^{\max}, & i = 1, ..., N_{PQ} \\ &S_{L_{i}} \leq S_{L_{i}}^{\max}, & i = 1, ..., N_{L}(11) \end{aligned} \tag{9}$$

Where N<sub>G</sub>, N<sub>PO</sub> and N<sub>L</sub> are the number of generator buses, the number of PQ buses, and the number of load buses respectively.

#### III. Differential Evolution - Overview

Differential evolution algorithm was proposed by Storn and Price [4] in 1995 to solve real parameter optimization problems. DE is also a population based searching algorithm and the optimization process involves following four steps.

#### Initialization

All independent variables are initialized randomly within their feasible numerical range between 0 and 1. NP is the population size. D is the control variables which are going to be optimized. It is initialized using the MATLAB function in eqn. (12)

#### Mutation

After initialization, the mutation operation is applied to generate the mutant vector Yi for each target vector Xi in the current population. In order to explore the search space, difference vector is added to the base vector. The mutation equation is given eqn. (13).

$$Y_i(G) = X_{i1}(G) + F * (X_{i2}(G) - X_{i3}(G)) (13)$$

Where F is the mutation scaling factor,  $F \in \{0, 1\}$ .

#### Crossover

After mutation process, to increase the diversity of the current population, DE performs the crossover operation to produce the trail vector. Two types of crossover schemes can be used with DE. These are exponential crossover and binomial crossover. The binomial variant was widely used in different applications [6].

binomial variant was widely used in different applications [6]. 
$$U_{i,j}(t) = \begin{cases} Y_{i,j}(t) & \text{if } \operatorname{rand}_{k,i} \leq \operatorname{CR} \text{ or } k = \operatorname{I}_{\operatorname{rand}} \\ X_{i,j}(t) & \text{if } \operatorname{rand}_{k,i} \leq \operatorname{CR} \text{ or } k = \operatorname{I}_{\operatorname{rand}} \end{cases} \tag{14}$$

rand\_k, i  $\epsilon$  [0, 1], I<sub>rand</sub> is chosen randomly from the interval [1 . . . D] once for each vector to ensure that at least one vector component originates from the mutated vector  $Y_i$ . CR is the crossover control parameter between 0 and 1.

#### Selection

The selection operation selects, according to the fitness value of the population vector and its corresponding trail vector. For minimization problem the vector; which is having the lower fitness value is chosen. All solutions in the population have the same chance of being selected as parents.

$$X_{i,j}(t+1) = \begin{cases} U_i(t) & \text{if } f(U_i(t)) \le f(X_i(t)) \\ X_i(t) & \text{if } f(X_i(t)) \le f(U_i(t)) \end{cases}$$
(15)

#### 3.1. Need For New variants of DE

The main control parameters of DE are (i) Mutation scaling factor (F) (ii) Crossover ratio (CR) (iii) Number of population (NP). They have a large impact on performance of the algorithm. Selecting suitable value of F and CR is a tedious process. To avoid that situation, many literatures suggest F and CR should be adaptive in each generation. This adaptive nature improves the performance of the DE algorithm. So far many variants are introduced in the literature concentrated on the F.

#### IV. SELF-BALANCED DIFFERENTIAL EVOLUTION

In this section, new variant of DE, named SBDE is presented. It is proposed by Harish Sharma [11] in 2014. Exploration and exploitation are the important terms in optimization. Exploration means expanding the search space, i.e. global search, on the other hand, exploitation means search around the good solution i.e. local search. To maintain the proper balance between the exploration and exploitation, a new mutation operation is introduced. It is given in equation (16).

$$Y_i(G) = C * X_{i1}(G) + F * (X_{i2}(G) - X_{i3}(G))(16)$$

G is the generation counter

C is the Cognition Learning Factor

It is dynamic based on the probability of fitness. Its value is calculated using eqn. (17).

$$Fi (G + 1) = (rand(0,1) - 0.5) * (1.5 - prob_i (G))$$
 (17)

In the above equation probability is calculated using eqn. (18).

$$prob_{i}(G) = \frac{0.9*fitness(G)}{maxfit(G)} + 0.1$$
 (18)

C varies between [0.1-1] according to the fitness of an individual X and it is the most important parameter in SBDE. It controls the balance between exploration and exploitation capabilities of the algorithm. Furthermore, the range of scale factor F is also dynamically varied. The dynamic scale factor controls the differentiation rate in mutation process in a better way. By

varying C and F, exploration and exploitation capabilities of DE can be balanced. So it is named as Self Balanced Differential Evolution (SBDE).

### 4.1 Application of SBDE to solve reactive dispatch problem

The following sections explain the constraints handling mechanism and implementation of SBDE on the ORPD problem.

#### 4.2 Constraint handling mechanism

It is worth mentioning that during the process of optimization, all the constraints are satisfied as follows.

- (a) The load flow equality constraints are satisfied by Newton Raphson (NR) power flow algorithm.
- (b) The generator bus voltage  $(V_{Gi})$ , transformer tap setting  $(T_i)$  and switchable reactive power compensations  $(Q_{Ci})$  are control variables and these are self-restricted between their respective minimum and maximum values by the algorithm.
- (c) State variables constraints: The most common approach in the DE to handle constraints is to use penalties because they are simple and easy to implement.

#### 4.3 Penalty Function Method

In this method of constraint handling [8], the fitness function is defined as the sum of the objective function f(x) and a penalty term which depends on the constraint violation. Most commonly used representation is given in eqn. (19).

used representation is given in eqn. (19). 
$$F = f + R_1 (P_{G_1} - P_{G_1}^{lim})^2 + \sum_{i=1}^{N_{PQ}} R_2 (V_{Li} - V_{Li}^{lim})^2 + \sum_{i=1}^{N_G} R_3 (Q_{G_i} - Q_{G_i}^{lim})^2 + \sum_{i=1}^{N_L} R_4 (|S_L - S_L^{max}|)^2$$
(19)

R1, R2, R3, R4 are penalty coefficient associated with real power generation, bus voltage magnitude, reactive power generation and apparent line flow limit violation respectively. The value of penalty coefficients can be fixed only by trial and error method and also problem depended.

The step by step procedure of implementation of SBDE algorithm for solving RPD is as follows.

#### 4.4 Algorithm

- Simulation parameters of SBDE, Number of Population (NP), scaling factor (F), Crossover (CR), Number of control variables (D), lower and upper limit of control variables (L & U), and maximum number of iteration are defined.
- An initial population Xi is generated randomly using eqn. (12).
- Run NR power flow available in MATPOWER package and calculate the objective function value (PLoss1).
- 4. Start iteration counter G=1.
- 5. Find probability of each individual's according to eqn. (18).
- Perform mutation operation to generate donor vector according to eqn. (16).
- 7. Perform crossover operation to generate trail vector according to eqn. (14).
- Run NR power flow and calculate the objective function value (P<sub>Loss2</sub>) for trail vector.
- For each individual's compare the objective functions value of initial and trail vectors.
- 10. If trail vector dominates the initial vector according to eqn. (15), update the value of C for next generation and trail

- vector replaces the target vector and go to step 14, otherwise continue.
- 11. When an individual is not updated re-initialize the individuals and set C value equal to 0.1 otherwise retains the previous value.
- 12. Same target vector is selected for next generation.
- 13. Calculate the value of F according to eqn. (17).
- 14. If the current iteration number reaches the predefined maximum iteration, stop the process. Otherwise go to step

The flowchart of the proposed SBDE based ORPD is illustrated in Fig. 1.

#### V. RESULTS AND DISCUSSIONS

In order to demonstrate the efficiency and robustness of the proposed SBDE algorithm, it is first tested on standard IEEE-57 bus test system and then in IEEE-118 bus system. The generator voltages ( $V_G$ ), transformer tap settings ( $T_i$ ) and reactive power injections ( $Q_C$ ) are taken as control variables. MATLAB program is written for SBDE algorithm and the power flow is calculated using MATPOWER 5.0 package. The details of control variables and their limits are given in Table I. The Parameters used for the simulation are summarized in Table II.

#### 5.1 IEEE 57-bus system

The topology and the system data of the IEEE 57-bus system can be found in [27]. The network consists of 80 branches, seven generator buses and 50 load buses. Fifteen branches 4-18,4-18, 21-20,24-26, 7-29, 34-32,11-41, 15-45,14-46,10-51, 13-49, 11-43,40-56, 39-57, 9-55have tap changing transformers. The buses with possible reactive power source installations are given in Table II. The available reactive powers of capacitor banks are within the interval 5 to 10MVAr. It also gives the details of the control variables and their maximum and minimum limits.

#### 5.2 Case A: Base Load Condition(PLoss)

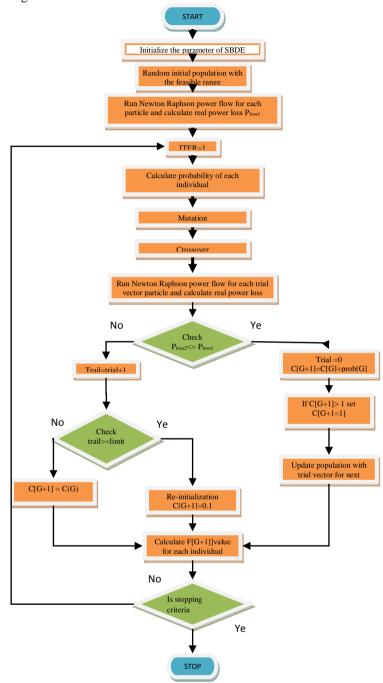
In this case, RPD problem is solved by the proposed method with base load condition load bus voltage limit is taken as (0.94-1.06) p.u.

#### 5.2.1 Case A1:Minimization of Real Power Loss (PLoss)

In this case, the SBDE algorithm is run with minimization of real power losses as the objective function Fig.2 shows the convergence characteristic of the performance of the optimization technique in terms of  $P_{loss}$ .

Table III gives the details of the control variables and P<sub>loss</sub>after optimization. The results obtained by SBDE approach is compared with the results those reported in literature like OGSA[16], GSA [15], nonlinear programming (NLP) [17], canonical GA (CGA) [17], Adaptive GA (AGA) [17], PSO with adaptive inertia weightweight (PSO-w) [17], PSO with a constriction factor (PSO-cf) [17], CLPSO [17], a real standard version of PSO, called as SPSO-07 [17], DEs with local search, instead of their corresponding original versions and denoted as L-DE [17],L-SACP-DE [17], LSaDE [17],SOA [17], BBO [14],BBO (after relaxing Q-limit of bus 2 and 9) [14] for the

Fig. 1. Flowchart for SBDE based ORPD



same IEEE 57 test system. The results of the comparison are given in Table III.From the comparison, the proposed SBDE algorithm gives the minimum loss that shows the better performance of the SBDE algorithm.

Table I.Details of control variables for IEEE 57 bus system

Variable	Bus/branch no.	Minimum limit	Maximum limit
Generator bus voltage	1,2,3,6,8,9,12	0.94 p.u	1.06 p.u
Transformer tap position	Branch 4-18, 4- 18, 21-20,24-26, 7-29, 34-32,11- 41, 15-45, 14- 46,10-51, 13-49, 11-43,40-56, 39- 57, 9-55	0.9p.u	1.1p.u
Q power source installation	10,12, 15, 17, 20, 21, 23, 24, 29	5Mvar	10Mvar

Table II. Simulation parameters for IEEE 57 bus

Parameter	Value
No. of population (NP)	100
Scaling Factor(F)	0.8
Crossover Ratio(CR)	0.8
Maximum No. of iteration	500

### **5.2.2** Case A2: Minimization of Total Voltage Deviations (TVD):

In this case, the proposed SBDE approach is applied for the improvement of voltage profile in the objective function (TVD), the results obtained from the proposed SBDE method for optimal settings of the control variables are given in Table IV. The total voltage deviations are decreased from base case value of 1.23358 to 0.6396 with a reduction of 48.15%. Fig.3 shows the convergence characteristic of the performance of the optimization technique in terms of Voltage Deviations with SBDE for the best run out of 30 trials. The proposed SBDE is found to be performing better than OSGA [16]. The comparison between SBDE and OSGA is listed in Table IV.It is also important that time taken for convergence by SBDE is lesser than OSGA.

#### 5.3 130% of base load

In order to analyze the system under stressed conditions, the active and reactive loads of each bus are increased to 130% of the base load condition. In this case all load bus voltage limit is taken as (0.94-1.06) p.u. Two Different objective functions are considered separately such as minimization of real power loss and total voltage deviations.

#### 5.3.1 Case B1: Minimization of Real Power Loss (PLoss)

The system performance like optimum control variables before and after optimization using SBDE is given in third column of Table V. Fig. 4 shows the convergence characteristic of the performance of the optimization technique in terms of  $P_{loss}$  with SBDE. The resultshows real power loss value is decreased from 85.22 MW to 75.45 MW with a reduction of 11.46%. These optimistic results are good indication that the system relieving from the stressed condition to a better levelout of 30 trials. It is clear from Fig.4 the real power loss values are significantly reduced with proposed approach. Also this

significant reduction shows the dominance of the proposed approach. It can be observed that the performance and robustness of SBDE algorithm is better than the other algorithm for the system under stressed condition.

### 5.3.2 Case B2: Minimization Of Total Voltage Deviations(TVD):

The results obtained from the proposed SBDE method for optimal settings of the control variables are given in the fourth column of Table V. The total voltage deviations are decreased from base case value of **1.5415** to **1.0239** with a reduction of **33.6** % under stressed condition. Fig. 5 shows the convergence characteristics of IEEE-57 bus for voltage deviation under stressed condition.

Fig.2 Convergence characteristics forPloss minimization (caseA1)

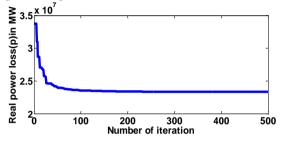


Fig.3 Convergence characteristics of VD minimization (Case A2)

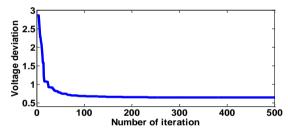


Fig.4 Convergence characteristics of loss minimization (case B1)

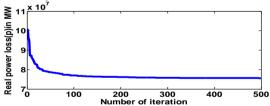
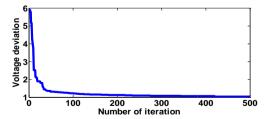


Fig.5 Convergence characteristics of VD minimization (Case B2)



 $Table \ III. Comparison \ of \ simulation \ results \ for \ IEEE \ 57-bus \ test \ power \ system \ with \ P_{loss}minimization (Case \ A1) \\ NR*\ means \ Not \ reported$ 

	CLPSO[17]	PSO-07[17]	L-DE[17]	L-SACP-DE[17]	L-SaDE[17]	SOA[17]	BBO[14]	BBO*[14]
				Generator voltage		201-[17]		
V <sub>1</sub> ,p.u	1.0541	1.0596	1.0397	0.9884	1.0600	1.0600	1.0600	1.0600
V <sub>2</sub> ,p.u	1.0529	1.0580	1.0463	1.0543	1.0574	1.0580	1.0504	1.0580
V <sub>3</sub> ,p.u	0.0337	1.0488	1.0511	1.0278	1.0438	1.0437	1.0440	10442
V <sub>6</sub> ,p.u	0.0313	1.0362	1.0236	0.9672	1.0364	1.0352	1.0376	1.0364
V <sub>8</sub> ,p.u	1.0496	1.06	1.0538	1.0552	1.0537	1.0458	1.0550	1.0567
V <sub>9</sub> ,p.u	1.0302	1.0433	0.94518	1.0245	1.0366	1.0369	1.0229	1.0377
V <sub>12,</sub> p.u	1.0342	1.0356	0.99078	1.0098	1.0323	1.0336	1.0323	1.0351
Transformer tap		1	•		1	1	1	1
$T_{4-18}$	0.99	0.95	1.02	1.05	0.94	1.00	0.96693	0.99165
$T_{4-18}$	0.98	0.99	0.91	1.05	1.00	0.96	0.99022	0.96447
T <sub>21-20</sub>	0.99	0.99	0.97	0.95	1.01	1.01	1.0120	1.0122
T <sub>24-26</sub>	1.01	1.02	0.91	0.98	1.01	1.01	1.0087	1.0110
T <sub>7-29</sub>	0.99	0.97	0.96	0.97	0.97	0.97	0.97074	0.97127
T <sub>34-32</sub>	0.93	0.96	0.99	1.09	0.97	0.97	0.96869	0.97227
T <sub>11-41</sub>	0.91	0.92	0.98	0.92	0.9	0.90	0.90082	0.90095
T <sub>15-45</sub>	0.97	0.96	0.96	0.91	0.97	0.97	0.96602	0.97063
T <sub>14-46</sub>	0.95	0.95	1.05	1.08	0.96	0.95	0.95079	0.95153
T <sub>10-51</sub>	0.98	0.97	1.07	0.99	0.96	0.96	0.96414	0.96252
T <sub>13-49</sub>	0.95	0.92	0.99	0.91	0.92	0.92	0.92462	0.92227
T <sub>11-43</sub>	0.95	1.00	1.06	0.94	0.96	0.96	0.95022	0.95988
T <sub>40-56</sub>	1.00	1.00	0.99	0.99	1.00	1.00	0.99666	1.0018
T <sub>39-57</sub>	0.96	0.95	0.96	0.96	0.96	0.96	0.96289	0.96567
T <sub>9-55</sub>	0.97	0.98	1.1	1.1	0.97	0.97	0.96001	0.97199
Capacitor banks	0.00000	0.02026	0		0.00112	0.00004	0.00702	0.00640
Q <sub>C-18</sub> ,p.u	0.09888	0.03936	0	0	0.08112	0.09984	0.09782	0.09640
Q <sub>C-25</sub> ,p.u	0.05424	0.05664	0	0	0.05808	0.05904	0.058991	0.05897
Q <sub>C-53</sub> ,p.u	0.0.6288	0.03552	0 070126	0	0.06192	0.06288	0.6289	0.062948
P <sub>loss</sub> ,p.u	0.2451520	0.2774430	0.278126	0.2791553	0.2426739	0.2426548	0.24544	0.242616
TVD,p.u	NR* 423.30	NR*	NR*	NR*	NR*	NR* 382.23	NR* NR*	NR* NR*
CPU time ,s	423.30	421.98	426.97	427.23	408.97	382.23	NK**	NK**
Variable	SBDE	OGSA[16]	GSA[15]	NLP[17]	CGA[17]	AGA[17]	PSO-w[17]	PSO-d[17]
Generator voltag			[ . ]			- [ . ]		
V <sub>1</sub> ,p.u	1.0600	1.0600	1.06000	1.06	0.9686	1.0276	1.06	1.06
V <sub>2</sub> ,p.u	1.0591	1.0594	1.06000	1.06	1.0493	1.0117	1.0578	1.0586
V <sub>3</sub> ,p.u	1.0494	1.0492	1.06000	1.0538	1.0567	1.0335	1.04378	1.0151
	1.0474	1.0492	1.00000				1.04376	1.0464
$V_{6}$ ,p.u	1.0436	1.0492	1.00810	1.06	0.9877	1.0010	1.04578	1.0464
V <sub>6</sub> ,p.u V <sub>8</sub> ,p.u								
V <sub>6</sub> ,p.u V <sub>8</sub> ,p.u V <sub>9</sub> ,p.u	1.0436	1.0433	1.00810	1.06	0.9877	1.0010	1.0356	1.0415
V <sub>8</sub> ,p.u	1.0436 1.0599	1.0433 1.0600	1.00810 1.05495	1.06 1.06	0.9877 1.0223	1.0010 1.0517	1.0356 1.0546	1.0415 1.06
V <sub>8</sub> ,p.u V <sub>9</sub> ,p.u	1.0436 1.0599 1.0454 1.0416	1.0433 1.0600 1.0450	1.00810 1.05495 1.00980	1.06 1.06 1.06	0.9877 1.0223 0.9918	1.0010 1.0517 1.0518	1.0356 1.0546 1.0369	1.0415 1.06 1.0423
$V_{8},p.u$ $V_{9},p.u$ $V_{12},p.u$ $Transformer\ tap$ $T_{4-18}$	1.0436 1.0599 1.0454 1.0416	1.0433 1.0600 1.0450	1.00810 1.05495 1.00980	1.06 1.06 1.06	0.9877 1.0223 0.9918	1.0010 1.0517 1.0518	1.0356 1.0546 1.0369	1.0415 1.06 1.0423
$V_8,p.u$ $V_9,p.u$ $V_{12},p.u$ $Transformer tap$ $T_{4-18}$ $T_{4-18}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263	1.06 1.06 1.06 1.06 1.06	0.9877 1.0223 0.9918 1.0044 0.92 0.92	1.0010 1.0517 1.0518 1.0570 1.03 1.02	1.0356 1.0546 1.0369 1.0334 0.90 1.02	1.0415 1.06 1.0423 1.0371 0.98 0.98
$V_8$ ,p.u $V_9$ ,p.u $V_{12}$ ,p.u Transformer tap	1.0436 1.0599 1.0454 1.0416 ratio 0.9001	1.0433 1.0600 1.0450 1.0407	1.00810 1.05495 1.00980 1.018591 1.10000	1.06 1.06 1.06 1.06 0.91	0.9877 1.0223 0.9918 1.0044	1.0010 1.0517 1.0518 1.0570	1.0356 1.0546 1.0369 1.0334	1.0415 1.06 1.0423 1.0371
$V_8,p.u$ $V_9,p.u$ $V_{12},p.u$ $Transformer tap$ $T_{4-18}$ $T_{4-18}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673	1.06 1.06 1.06 1.06 1.06	0.9877 1.0223 0.9918 1.0044 0.92 0.92	1.0010 1.0517 1.0518 1.0570 1.03 1.02	1.0356 1.0546 1.0369 1.0334 0.90 1.02	1.0415 1.06 1.0423 1.0371 0.98 0.98
$V_{8,p.u}$ $V_{9,p.u}$ $V_{12,p.u}$ Transformer tap $T_{4-18}$ $T_{4-18}$ $T_{21-20}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9001 0.9111	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08	0.9877 1.0223 0.9918 1.0044 0.92 0.92 0.92	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01
$V_{8}, p. u \\ V_{9}, p. u \\ V_{12}, p. u \\ Transformer tap \\ T_{4-18} \\ T_{21-20} \\ T_{24-26} \\ T_{7-29} \\ T_{34-32}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9001 0.9111 0.9000	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09	0.9877 1.0223 0.9918 1.0044 0.92 0.92 0.97 0.90 0.91 1.1	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.99
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ \hline V_{12}, p.u \\ \hline Transformer tap \\ T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9001 0.9111 0.9000 0.9000	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92	0.9877 1.0223 0.9918 1.0044 0.92 0.92 0.97 0.90 0.91 1.1 0.94	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.90	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ \hline V_{12}, p.u \\ \hline Transformer tap \\ T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.901 0.9111 0.9000 0.9000 0.9000	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91	0.9877 1.0223 0.9918 1.0044 0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.90 0.97	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ \hline V_{12}, p.u \\ \hline Transformer tap \\ T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{14-46} \\ \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.901 0.9111 0.9000 0.9000 0.9000 1.0464	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91 0.98	0.9877 1.0223 0.9918 1.0044 0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.99 0.97	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ \hline V_{12}, p.u \\ \hline Transformer tap \\ \hline T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{14-46} \\ \hline T_{10-51} \\ \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.901 0.9111 0.9000 0.9000 0.9000 1.0464 0.9875	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91 0.98	0.9877 1.0223 0.9918 1.0044 0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.90 0.97	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97
$\begin{array}{c} V_{8,p.u} \\ V_{9,p.u} \\ V_{12,p.u} \\ \hline Transformer tap \\ \hline T_{4-18} \\ \hline T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{14-46} \\ \hline T_{10-51} \\ \hline T_{13-49} \\ \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.901 0.9111 0.9000 0.9000 0.9000 1.0464 0.9875 0.9638	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91 0.98 0.98	0.9877 1.0223 0.9918 1.0044 0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.05	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.90 0.97 0.95 0.96 0.92	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.93
$\begin{array}{c} V_{8,p.u} \\ V_{9,p.u} \\ V_{12,p.u} \\ \hline Transformer tap \\ \hline T_{4.18} \\ \hline T_{4.18} \\ \hline T_{21.20} \\ \hline T_{24.26} \\ \hline T_{7.29} \\ \hline T_{34.32} \\ \hline T_{11.41} \\ \hline T_{15.45} \\ \hline T_{14.46} \\ \hline T_{10.51} \\ \hline T_{13.49} \\ \hline T_{11.43} \\ \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 0.9000	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.901 0.9111 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91 0.98 0.98 0.98	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.05 0.95	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.90 0.97 0.95 0.96 0.92 0.96	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.93 0.97
$\begin{array}{c} V_{8,p.u} \\ V_{9,p.u} \\ \hline V_{12,p.u} \\ \hline Transformer tap \\ \hline T_{4.18} \\ \hline T_{4.18} \\ \hline T_{21.20} \\ \hline T_{24.26} \\ \hline T_{7.29} \\ \hline T_{34.32} \\ \hline T_{11.41} \\ \hline T_{15.45} \\ \hline T_{14.46} \\ \hline T_{10.51} \\ \hline T_{13.49} \\ \hline T_{11.43} \\ \hline T_{11.43} \\ \hline T_{40.56} \\ \hline \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 0.9000 1.0139	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9001 0.9111 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 0.9000	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91 0.98 0.98 0.98	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.05 0.95 1.05	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.95 0.96 0.92 0.96 1.00	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.93 0.97 0.99
$\begin{array}{c} V_{8,p.u} \\ V_{9,p.u} \\ \hline V_{12,p.u} \\ \hline Transformer tap \\ \hline T_{4.18} \\ \hline T_{4.18} \\ \hline T_{21.20} \\ \hline T_{24.26} \\ \hline T_{7.29} \\ \hline T_{34.32} \\ \hline T_{11.41} \\ \hline T_{15.45} \\ \hline T_{14.46} \\ \hline T_{10.51} \\ \hline T_{13.49} \\ \hline T_{11.43} \\ \hline T_{11.43} \\ \hline T_{40.56} \\ \hline T_{39.57} \\ \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 0.9000 1.0139 0.9824	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9011 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 0.9000 1.0148	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999 1.02465	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91 0.98 0.98 0.98 0.98 1.08	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 0.90 1.00 0.96	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.05 0.95 1.05 0.99	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.95 0.96 0.92 0.96 1.00 0.96	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.93 0.97 0.99 0.96
$\begin{array}{c} V_{8,p.u} \\ V_{9,p.u} \\ V_{12,p.u} \\ \hline Transformer tap \\ \hline T_{4.18} \\ \hline T_{4.18} \\ \hline T_{21.20} \\ \hline T_{24.26} \\ \hline T_{7.29} \\ \hline T_{34.32} \\ \hline T_{11.41} \\ \hline T_{15.45} \\ \hline T_{14.46} \\ \hline T_{10.51} \\ \hline T_{13.49} \\ \hline T_{11.43} \\ \hline T_{40.56} \\ \hline T_{39.57} \\ \hline T_{9.55} \\ \hline \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 0.9000 1.0139	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9001 0.9111 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 0.9000	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999	1.06 1.06 1.06 1.06 1.06 0.91 1.06 0.93 1.08 1.00 1.09 0.92 0.91 0.98 0.98 0.98	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.05 0.95 1.05	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.95 0.96 0.92 0.96 1.00	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.93 0.97 0.99
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ \hline V_{12}, p.u \\ \hline Transformer tap \\ \hline T_{4-18} \\ \hline T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{14-46} \\ \hline T_{10-51} \\ \hline T_{13-49} \\ \hline T_{11-43} \\ \hline T_{40-56} \\ \hline T_{39-57} \\ \hline T_{9-55} \\ \hline Capacitor banks \\ \hline \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 1.0139 0.9824 0.9021	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9011 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 0.9000 1.0148 0.9830	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999 1.02465 1.03731	1.06 1.06 1.06 1.06 1.06 1.06 1.06 0.91 1.08 1.00 1.09 0.92 0.91 0.98 0.98 0.98 0.98 1.08 1.08 1.08	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00 0.90 1.00	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.05 0.95 1.01 0.94 1.00	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.95 0.96 0.92 0.96 1.00 0.96 0.98	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.99 0.97 0.99 0.98
$\begin{array}{c} V_{8,p.u} \\ V_{9,p.u} \\ V_{12,p.u} \\ \hline Transformer tap \\ \hline T_{4.18} \\ \hline T_{4.18} \\ \hline T_{21.20} \\ \hline T_{24.26} \\ \hline T_{7.29} \\ \hline T_{34.32} \\ \hline T_{11.41} \\ \hline T_{15.45} \\ \hline T_{14.46} \\ \hline T_{10.51} \\ \hline T_{13.49} \\ \hline T_{11.43} \\ \hline T_{40.56} \\ \hline T_{39.57} \\ \hline T_{9.55} \\ \hline Capacitor banks \\ Q_{C.18,p.u} \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 1.0139 0.9824 0.9021	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9011 0.9000 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 0.9000 1.0148 0.9830	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999 1.02465 1.03731	1.06 1.06 1.06 1.06 1.06 1.06 0.91 1.08 1.00 1.09 0.92 0.91 0.98 0.98 0.98 0.98 1.08 1.08	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00 0.96 1.00	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.05 0.95 1.01 0.94 1.00	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.99 0.95 0.96 1.00 0.96 0.98	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.99 0.99 0.99 0.99 0.99 0.99
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ V_{12}, p.u \\ \hline Transformer tap \\ \hline T_{4-18} \\ \hline T_{4-18} \\ \hline T_{2-120} \\ \hline T_{2-4-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{14-46} \\ \hline T_{10-51} \\ \hline T_{13-49} \\ \hline T_{11-43} \\ \hline T_{40-56} \\ \hline T_{39-57} \\ \hline T_{9-55} \\ \hline Capacitor banks \\ Q_{C-18}, p.u \\ Q_{C-25}, p.u \\ \hline \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 1.0139 0.9824 0.9021	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9011 0.9000 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 1.0148 0.9830	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999 1.02465 1.03731	1.06 1.06 1.06 1.06 1.06 1.06 1.06 1.06	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00 0.96 1.00 0.084 0.00816	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.01 0.94 1.00 0.0168 0.01536	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.99 0.97 0.95 0.96 0.92 0.96 1.00 0.96 0.98	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.99 0.99 0.99 0.99 0.99 0.99 0.99
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ V_{12}, p.u \\ \hline Transformer tap \\ \hline T_{4-18} \\ \hline T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{10-51} \\ \hline T_{13-49} \\ \hline T_{11-43} \\ \hline T_{40-56} \\ \hline T_{39-57} \\ \hline T_{9-55} \\ \hline Capacitor banks \\ Q_{C-18}, p.u \\ Q_{C25}, p.u \\ Q_{C5-3}, p.u \\ \hline \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 1.0139 0.9824 0.9021	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9011 0.9000 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 1.0148 0.9830	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999 1.02465 1.03731 0.07825 0.005869 0.046872	1.06 1.06 1.06 1.06 1.06 1.06 1.06 1.06	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00 0.96 1.00 0.084 0.00816 0.05376	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.01 0.94 1.00 0.0168 0.01536 0.03888	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.90 0.97 0.95 0.96 0.92 0.96 1.00 0.96 0.98	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.99 0.99 0.97 0.99 0.99 0.99 0.99
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ V_{12}, p.u \\ \hline Transformer tap \\ \hline T_{4-18} \\ \hline T_{4-18} \\ \hline T_{2-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{10-51} \\ \hline T_{13-49} \\ \hline T_{11-43} \\ \hline T_{13-49} \\ \hline T_{20-51} \\ \hline T_{20-5$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 0.9000 1.0139 0.9824 0.9021 9.8684 9.9999 9.9759 0.2333	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9011 0.9000 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 1.0148 0.9830 0.0682 0.0590 0.0630 0.2343	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999 1.02465 1.03731 0.07825 0.005869 0.046872 0.234611	1.06 1.06 1.06 1.06 1.06 1.06 1.06 1.06	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00 0.96 1.00 0.084 0.00816 0.05376 0.2524411	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.01 0.94 1.00 0.0168 0.01536 0.03888 0.24564	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.90 0.97 0.95 0.96 0.92 0.96 1.00 0.96 0.98 0.05136 0.05904 0.06288 0.242702	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.99 0.97 0.99 0.98 0.97 0.99 0.98 0.99 0.98 0.98
$\begin{array}{c} V_{8}, p.u \\ V_{9}, p.u \\ V_{12}, p.u \\ \hline Transformer tap \\ \hline T_{4-18} \\ \hline T_{4-18} \\ \hline T_{21-20} \\ \hline T_{24-26} \\ \hline T_{7-29} \\ \hline T_{34-32} \\ \hline T_{11-41} \\ \hline T_{15-45} \\ \hline T_{10-51} \\ \hline T_{13-49} \\ \hline T_{11-43} \\ \hline T_{40-56} \\ \hline T_{39-57} \\ \hline T_{9-55} \\ \hline Capacitor banks \\ Q_{C-18}, p.u \\ Q_{C25}, p.u \\ Q_{C5-3}, p.u \\ \hline \end{array}$	1.0436 1.0599 1.0454 1.0416 ratio 0.9001 0.9006 0.9785 0.9833 0.9001 0.9539 0.9012 0.9014 0.9022 0.9166 0.9000 1.0139 0.9824 0.9021	1.0433 1.0600 1.0450 1.0407 0.9000 0.9947 0.9000 0.9011 0.9000 0.9000 0.9000 1.0464 0.9875 0.9638 0.9000 1.0148 0.9830	1.00810 1.05495 1.00980 1.018591 1.10000 1.08263 0.92198 1.01673 0.99626 1.10000 1.07462 0.95434 0.93772 1.01679 1.05257 1.10000 0.97999 1.02465 1.03731 0.07825 0.005869 0.046872	1.06 1.06 1.06 1.06 1.06 1.06 1.06 1.06	0.9877 1.0223 0.9918 1.0044  0.92 0.92 0.97 0.90 0.91 1.1 0.94 0.95 1.03 1.09 0.90 0.90 1.00 0.96 1.00 0.084 0.00816 0.05376	1.0010 1.0517 1.0518 1.0570 1.03 1.02 1.06 0.99 1.10 0.98 1.01 1.08 0.94 0.95 1.01 0.94 1.00 0.0168 0.01536 0.03888	1.0356 1.0546 1.0369 1.0334 0.90 1.02 1.01 1.01 0.97 0.97 0.90 0.97 0.95 0.96 0.92 0.96 1.00 0.96 0.98	1.0415 1.06 1.0423 1.0371 0.98 0.98 1.01 1.01 0.98 0.97 0.90 0.97 0.96 0.97 0.99 0.99 0.97 0.99 0.99 0.99 0.99

Table IV. Simulation results for IEEE-57 bus TVD minimization(Case A2)

Variable	SBDE	OGSA[16]
Generator voltage		
V <sub>1</sub> ,p.u	1.0269	1.0138
V <sub>2</sub> ,p.u	1.0163	0.9608
V <sub>3,</sub> p.u	1.0124	1.0173
V <sub>6</sub> ,p.u	1.0012	0.9898
V <sub>8</sub> ,p.u	1.0303	1.0362
V <sub>9</sub> ,p.u	1.0255	1.0241
V <sub>12</sub> ,p.u	1.0016	1.0136
Transformer tap ratio		
T <sub>4-18</sub>	1.0141	0.9833
T <sub>4-18</sub>	0.9872	0.9503
T <sub>21-20</sub>	0.9784	0.9523
T <sub>24-26</sub>	1.0161	1.0036
T <sub>7-29</sub>	0.9798	0.9778
T <sub>34-32</sub>	0.9174	0.9146
T <sub>11-41</sub>	0.9001	0.9454
T <sub>15-45</sub>	0.9240	0.9265
T <sub>14-46</sub>	0.9705	0.9960
$T_{10-51}$	1.0014	1.0386
T <sub>13-49</sub>	0.9001	0.9060
T <sub>11-43</sub>	0.9569	0.9234
T <sub>40-56</sub>	1.0315	0.9871
T <sub>39-57</sub>	0.9017	1.0132
T <sub>9-55</sub>	0.9929	0.9372
Capacitor banks		
Q <sub>C-18,p.u</sub>	9.9479	0.0463
Q <sub>C-25</sub> ,p.u	9.9970	0.0590
Q <sub>C-53</sub> ,p.u	9.9781	0.0628
P <sub>loss</sub> , MW	0.27521	0.3234
TVD,p.u	0.6396	0.6982
CPU time ,s	329.96	419.17

### 6.1 IEEE 118-bus system

The topology and the system data of the IEEE 118-bus system can be found in [28]. The network consists of 186 branches, fifty four generator buses and 64 load buses. Fifteen branches 8-5, 26-25, 30-17, 38-37, 63-59, 64-61, 65-66, 68-69,81-80 have tap changing transformers.

Table VI gives the details of the simulation parameters. The buses with possible reactive power source installations are given in Table VII. The available reactive powers of capacitor banks are within the interval 5 to 10MVAr.

Parameter	Value
No. of population (NP)	100
Scaling Factor(F)	0.8
Crossover Ratio(CR)	0.8
Maximum No. of iteration	500

Table VI. Simulation Parameters for IEEE-118 Bus

Table V. IEEE-57 bus Simulation results for case B1 and B2 (130 % increase in base load case)

Sl.No	Control Variables	Case B1(SBDE)	Case B2(SBDE)
1	V1	1.0600	1.0432
2	V2	1.0600	1.0240
3	V3	1.0599	1.0249
4	V6	1.0389	1.0022
5	V8	1.0600	1.0377
6	V9	1.0463	1.0322
7	V12	1.0502	1.0158
8	T 4-18	0.9007	0.9061
9	T 4-18	0.9011	1.0831
10	T 21-20	1.0012	0.9660
11	T 24-26	0.9804	1.0942
12	T 7-29	0.9002	0.9325
13	T 34-32	0.9519	0.9000
14	T 11-41	0.9001	0.9001
15	T 15-45	0.9000	0.9155
16	T 14-46	0.9000	0.9649
17	T 10-51	0.9178	0.9669
18	T 13-49	0.9001	0.9001
19	T 11-43	0.9000	0.9178
20	T 40-56	1.0298	1.0298
21	T 39-57	0.9788	0.9001
22	T 9-55	0.9012	1.0113
23	Qsh18	9.6384	8.0985
24	Qsh25	9.9997	9.9999
25	Qsh53	9.9976	9.9559
P <sub>loss</sub> (M	W)	75.457	83.255
T.V.D		3.9821	1.0239

Table VII.Control Variables of IEEE-118 Bus system

Variable	Bus/branch no.	Minim	Maximum
		um limit	limit
Generator bus voltage	1,4,6,8,10,12,15, 18,19,24,25,26,2 7,31,32,34,36,40 ,42,46,49,54,55, 56,59, 61,62,65,66,70,7 2,73,74,76,77,80 ,85,87,89,90,91, 92,99,100,103,1 04,105, 107,110,111,112	0.94 p.u	1.06 p.u
	, 113,116.		
Transformer tap position	Branch 8-5, 26- 25, 30-17,38-37, 63-59, 64-61,65- 66, 68-69,81-80.	0.9p.u	1.1p.u
Q power source installation	5,34,37,44,45,46 , 48,74,79,82,83, 105,107,110.	5 Mvar	10 Mvar

#### 6.2 Case C: Base Load Condition

In this case, RPD problem is solved by the proposed method with base load condition load bus voltage limit is taken as (0.94-1.06) p.u.

#### 6.2.1 Case C1:Minimization of Real Power Loss(PLoss)

In this case, the SBDE algorithm is run with minimization of real power losses as the objective function. Fig.6 shows the convergence characteristic of the performance of the optimization technique in terms of Ploss after optimization. The results obtained by SBDE approach is compared with the results those reported in literature like GSA[15], OGSA[16], CLPSO[24], PSO[24] for the same IEEE 118 test system. The results of the comparison are given in Table VIII. From the comparison, the proposed SBDE algorithm gives the minimum loss that shows the better performance of the SBDE algorithm compared to other algorithms. It can be observed that Plossreduces over the evolutions and converge to a minimum value from the base case value of 132.45 MW to 123.89MW with a reduction of 6.46 %. The results in the table VIII indicate the superiority of SBDE for larger power systems.

### 6.2.2 Case C2: Minimization of Total Voltage Deviations(TVD)

In this case, the proposed SBDE approach is applied for the improvement of voltage profile in the objective function (TVD), the results obtained from the proposed SBDE method for optimal settings of the control variables are given in Table IX. The total voltage deviations are decreased from base case value of 1.4393 to **0.3059** with a reduction of **78.74%**. Fig.7 showsthe convergence characteristic of the performance of the optimization technique in terms of Voltage Deviations with SBDE for the best run out of 30 trials. The proposed SBDE is found to be better than OSGA [16]. The comparison between SBDE and OSGA is listed in Table IX. The time taken for convergence is found to be lesser with SBDE than OSGA.

#### 6.3 130% of base load

In order to analyze the system under stressed conditions, the active and reactive loads of each bus are increased to 130% of the base load condition.

In this case all load bus voltage limit is taken as (0.94-1.06) p.u. Two Different objective functions are considered separately such as minimization of real power loss and total voltage deviations.

#### 6.3.1 Case D1: Minimization Of Real Power Loss(PLoss)

The system performance like optimum control variables before and after optimization using SBDE is given in Table X. Fig. 8 shows the convergence characteristic of the performance of the optimization technique in terms of  $P_{loss}$  with SBDE for the best run out of 30 trials. It is clear from Fig.8 the real power loss values are significantly reduced with proposed approach. The results shows real power loss value isdecreased from 335.02 MW to 310.98 MW. These optimistic results are good indication that the system relieving from the stressed condition to a better level reduction of 7.17%. The proposed algorithm performs well even under stressed condition.

Fig.6 Convergence characteristics of loss minimization(Case C1)

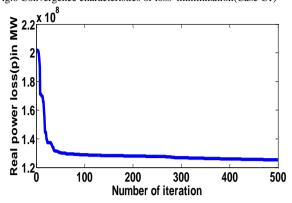


Fig.7 Convergence characteristics of VD minimization(Case C2)

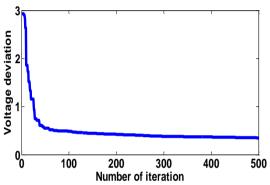


Fig.8 Convergence characteristics of loss minimization (Case D1)

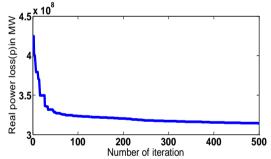
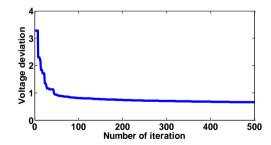


Fig.9 Convergence characteristics of VD minimization(Case D2)



 $Table\ VIII\ Comparison\ of\ simulation\ results of\ IEEE\ 118\ bus\ testpower\ system\ \ with\ P_{loss}\ minimization\ objective. (Case\ C1)$ 

Variable	SBDE	OGSA[16	GSA[15]	CLPSO[24]	PSO[24]	Variable	SBDE	OGSA[16]	GSA[15]	CLPSO[24]	PSO[24]
Generator	voltage		l .	1	L	Generator	voltage	1	1	1	l .
V <sub>1</sub> ,p.u	0.9994	1.0350	0.9600	1.0332	1.0853	V <sub>91</sub> ,p.u	1.0029	1.0297	1.0032	1.0288	0.9615
V <sub>4</sub> ,p.u	1.0154	1.0554	0.9620	1.0550	1.0420	V <sub>92</sub> ,p.u	1.0161	1.0353	1.0927	0.9760	0.9568
V <sub>6</sub> ,p.u	1.0132	1.0301	0.9729	0.9754	1.0805	V <sub>99</sub> ,p.u	1.0100	1.0395	1.0433	1.0880	0.9540
V <sub>8</sub> ,p.u	1.0214	1.0175	1.0570	0.9669	0.9683	V <sub>100</sub> ,p.u	1.0178	1.0275	1.0786	0.9617	0.9584
V <sub>10</sub> ,p.u	1.0506	1.0250	1.0885	0.9811	1.0756	V <sub>103</sub> ,p.u	1.0101	1.0158	1.0266	0.9611	1.0162
V <sub>12</sub> ,p.u	0.9991	1.0410	0.9630	1.0092	1.0225	V <sub>104</sub> ,p.u	0.9862	1.0165	0.9808	1.0125	1.0992
V <sub>15</sub> ,p.u	1.0038	0.9973	1.0127	0.9787	1.0786	V <sub>105</sub> ,p.u	0.9919	1.0197	1.0163	1.0684	0.9694
V <sub>18</sub> ,p.u	1.0037	1.0047	1.0069	1.0799	1.0498	V <sub>107</sub> ,p.u	0.9963	1.0408	0.9987	0.9769	0.9656
V <sub>19</sub> ,p.u	1.0054	0.9899	1.0003	1.0805	1.0776	V <sub>110</sub> ,p.u	0.9886	1.0288	1.0218	1.0414	1.0873
V <sub>24</sub> ,p.u	1.0089	1.0287	1.0105	1.0286	1.0827	V <sub>111</sub> ,p.u	0.9918	1.0194	0.9852	0.9790	1.0375
V <sub>25</sub> ,p.u	1.0208	1.0600	1.0102	1.0307	0.9564	V <sub>112</sub> ,p.u	0.9732	1.0132	0.9500	0.9764	1.0920
V <sub>26</sub> ,p.u	1.0600	1.0855	1.0401	0.9877	1.0809	V <sub>113</sub> ,p.u	1.0230	1.0386	0.9764	0.9721	1.0753
V <sub>27</sub> ,p.u	1.0107	1.0081	0.9809	1.0157	1.0874	V <sub>116</sub> ,p.u	1.0286	0.9724	1.0372	1.0330	0.9594
V <sub>31</sub> ,p.u	1.0136	0.9948	0.9500	0.9615	0.9608	Transform	er tap ratio	)			•
V <sub>32</sub> ,p.u	1.0063	0.9993	0.9552	0.9851	1.1000	T <sub>8</sub>	1.0037	0.9568	1.0659	1.0045	1.0112
V <sub>34</sub> ,p.u	1.0080	0.9958	0.9910	0.0157	0.9611	T <sub>32</sub>	1.0208	1.0409	0.9534	1.0609	1.0906
V <sub>36</sub> ,p.u	1.0043	0.9835	1.0091	1.0849	1.0367	T <sub>36</sub>	0.9961	0.9963	0.9328	1.0008	1.0033
V <sub>40</sub> ,p.u	1.0045	0.9981	0.9505	0.9830	1.0914	T <sub>51</sub>	1.0080	0.9775	1.0884	1.0093	1.0000
V <sub>42</sub> ,p.u	1.0014	1.0068	0.9500	1.0516	0.9701	T <sub>93</sub>	1.0125	0.9960	1.0579	0.9922	1.0080
V <sub>46</sub> ,p.u	0.9884	1.0355	0.9814	0.9754	1.0390	T <sub>95</sub>	0.9925	0.9956	0.9493	1.0074	1.0326
V <sub>49</sub> ,p.u	1.0077	1.0333	1.0444	0.9838	1.0836	T <sub>102</sub>	1.0015	0.9882	0.9975	1.0611	0.9443
V <sub>54</sub> ,p.u	0.9808	0.9911	1.0379	0.9637	0.9764	T <sub>107</sub>	1.0197	0.9251	0.9887	0.9307	0.9067
V <sub>55</sub> ,p.u	0.9879	0.9914	0.9907	0.9716	1.0103	T <sub>117</sub>	0.9823	1.0661	0.9801	0.9578	0.9673
V <sub>56</sub> ,p.u	0.9838	0.9920	1.0333	1.0250	0.9536	Capacitor	banks				
V <sub>59</sub> ,p.u	1.0140	0.9909	1.0099	1.0003	0.9672	Q <sub>C-5</sub> ,p.u	7.6611	-0.3319	0.00	0.0000	0.0000
V <sub>61</sub> ,p.u	1.0110	1.0747	1.0925	1.0771	1.0938	Q <sub>C-34</sub> ,p.u	8.7965	0.0480	7.46	11.7135	9.3639
V <sub>62</sub> ,p.u	1.0091	1.0753	1.0393	1.0480	1.0978	Q <sub>C-37</sub> ,p.u	7.5200	-0.2490	0.00	0.0000	0.0000
V <sub>65</sub> ,p.u	1.0366	0.9814	0.9998	0.9684	1.0892	Q <sub>C-44</sub> ,p.u	6.0547	0.0328	6.07	9.8932	9.3078
V <sub>66</sub> ,p.u	1.0162	1.0487	1.0355	0.9648	1.0861	Q <sub>C-45</sub> ,p.u	8.7156	0.0383	3.33	9.4169	8.6428
V <sub>69</sub> ,p.u	1.0370	1.0490	1.1000	0.9574	0.9665	Q <sub>C-46</sub> ,p.u	7.4596	0.0545	6.51	2.6719	8.9462
V <sub>70</sub> ,p.u	1.0133	1.0395	1.0992	0.9765	1.0783	Q <sub>C-48</sub> ,p.u	7.0826	0.0181	4.47	2.8546	11.809
V <sub>72</sub> ,p.u	1.0030	0.9900	1.0014	1.0243	0.9506	Q <sub>C-74</sub> ,p.u	8.2526	0.0509	9.72	0.5471	4.6132
V <sub>73</sub> ,p.u	1.0090	1.0547	1.0111	0.9651	0.9722	Q <sub>C-79</sub> ,p.u	10.000	0.1104	14.25	14.8532	10.592
V <sub>74</sub> ,p.u	1.0071	1.0167	1.0476	1.0733	0.9713	Q <sub>C-82</sub> ,p.u	7.4406	0.0965	17.49	19.4270	16.454
V <sub>76</sub> ,p.u	0.9955	0.9972	1.0211	1.0302	0.9602	Q <sub>C-83</sub> .p.u	7.0206	0.0263	4.28	6.9824	9.6325
V <sub>77</sub> ,p.u	1.0169	1.0071	1.0187	1.0275	1.0781	Q <sub>C-105</sub> ,p.u	7.4342	0.0442	12.04	9.0291	8.9513
V <sub>80</sub> ,p.u	1.0238	1.0066	1.0462	0.9857	1.0788	Q <sub>C-107</sub> ,p.u	7.1210	0.0085	2.26	4.9926	5.0426
V <sub>85</sub> ,p.u	1.0186	0.9893	1.0491	0.9836	0.9568	Q <sub>C-110</sub> ,p.u	8.9172	0.0144	2.94	2.2086	5.5319
V <sub>87</sub> ,p.u	0.9995	0.9693	1.0426	1.0882	0.9642	P <sub>loss</sub> ,MW	123.89	126.99	127.76	130.96	131.99
V <sub>89</sub> ,p.u	1.0314	1.0527	1.0955	0.9895	0.9748	TVD,p.u	0.8990	1.1829	NR*	NR*	NR*
V <sub>90</sub> ,p.u	1.0020	1.0290	1.0417	0.9905	1.0248	CPU,s	885.02	1152.32	1198.65	1472	1215
NR* means	Not repor	ted									

Table IX Comparison of simulation results for IEEE - 118 bus test power system with TVD minimization objective(Case C2)

Variable	SBDE	OGSA[16]	Variable	SBDE	OGSA[16]	Variable	SBDE	OGSA[16]
	Generator voltage							)
V <sub>1</sub> ,p.u	1.0033	1.0388	V <sub>65</sub> ,p.u	0.9828	0.9724	$T_8$	1.0079	0.9841
V <sub>4</sub> ,p.u	1.0159	0.9872	V <sub>66</sub> ,p.u	1.0100	1.0020	T <sub>32</sub>	1.0025	1.0377
V <sub>6</sub> ,p.u	0.9980	0.9925	V <sub>69</sub> ,p.u	0.9968	0.9827	T <sub>36</sub>	1.0053	0.9573
V <sub>8</sub> ,p.u	0.9800	0.9905	V <sub>70</sub> ,p.u	1.0053	0.9997	T <sub>51</sub>	0.9889	0.9952
V <sub>10</sub> ,p.u	0.9998	0.9919	V <sub>72</sub> ,p.u	0.9859	1.0123	T <sub>93</sub>	0.9788	0.9622
V <sub>12</sub> ,p.u	1.0053	1.0077	V <sub>73</sub> ,p.u	1.0135	0.9960	T <sub>95</sub>	1.0419	1.0320
V <sub>15</sub> ,p.u	1.0018	1.0034	V <sub>74</sub> ,p.u	1.0114	1.0232	T <sub>102</sub>	1.0160	1.0137
V <sub>18</sub> ,p.u	1.0024	0.9773	V <sub>76</sub> ,p.u	1.0113	1.0015	T <sub>107</sub>	1.0308	0.9795
V <sub>19</sub> ,p.u	1.0178	1.0324	V <sub>77</sub> ,p.u	1.0056	1.0124	T <sub>117</sub>	0.9592	0.9985
V <sub>24</sub> ,p.u	1.0053	1.0285	V <sub>80</sub> ,p.u	1.0226	1.0226		Capacitor banks	,

V <sub>25</sub> ,p.u	0.9991	0.9705	V <sub>85</sub> ,p.u	1.0060	1.0117	Q <sub>C-5</sub> ,p.u	7.9251	-0.2403
V <sub>26</sub> ,p.u	0.9734	1.0175	V <sub>87</sub> ,p.u	1.0142	1.0058	Q <sub>C-34</sub> ,p.u	9.0933	0.0371
V <sub>27</sub> ,p.u	1.0101	1.0117	V <sub>89</sub> ,p.u	1.0103	1.0076	Q <sub>C-37</sub> ,p.u	8.0202	-0.0437
V <sub>31</sub> ,p.u	1.0016	1.0014	V <sub>90</sub> ,p.u	0.9787	0.9753	Q <sub>C-44</sub> ,p.u	8.4524	0.0375
V <sub>32</sub> ,p.u	1.0011	0.9988	V <sub>91</sub> ,p.u	0.9986	0.9836	Q <sub>C-45</sub> ,p.u	7.1315	0.0400
V <sub>34</sub> ,p.u	1.0068	1.0158	V <sub>92</sub> ,p.u	1.0151	1.0272	Q <sub>C-46</sub> ,p.u	6.9449	0.0749
V <sub>36</sub> ,p.u	0.9999	0.9916	V <sub>99</sub> ,p.u	0.9856	0.9612	Q <sub>C-48</sub> ,p.u	7.4755	0.0796
V <sub>40</sub> ,p.u	1.0092	1.0132	V <sub>100</sub> ,p.u	1.0154	1.0032	Q <sub>C-74</sub> ,p.u	7.8995	0.0883
V <sub>42</sub> ,p.u	0.9974	0.9892	V <sub>103</sub> ,p.u	1.0095	0.9843	Q <sub>C-79</sub> ,p.u	8.6257	0.1218
V <sub>46</sub> ,p.u	1.0311	1.0607	V <sub>104</sub> ,p.u	0.9908	0.9880	Q <sub>C-82</sub> ,p.u	8.9486	0.0380
V <sub>49</sub> ,p.u	1.0077	1.0031	V <sub>105</sub> ,p.u	0.9999	1.0003	Q <sub>C-83</sub> .p.u	7.4944	0.0627
V <sub>54</sub> ,p.u	1.0234	1.0236	V <sub>107</sub> ,p.u	1.0104	1.0033	Q <sub>C-105</sub> ,p.u	8.2667	0.0459
V <sub>55</sub> ,p.u	1.0085	1.0176	V <sub>110</sub> ,p.u	1.0034	1.0040	Q <sub>C-107</sub> ,p.u	8.8299	0.0830
V <sub>56</sub> ,p.u	1.0103	1.0149	V <sub>111</sub> ,p.u	1.0165	1.0331	Q <sub>C-110</sub> ,p.u	7.2219	0.0221
V <sub>59</sub> ,p.u	0.9930	1.0584	V <sub>112</sub> ,p.u	0.9930	0.9877	P <sub>loss</sub> ,MW	160.77	157.72
V <sub>61</sub> ,p.u	1.0029	0.9829	V <sub>113</sub> ,p.u	1.0161	0.9705	TVD,p.u	0.3059	0.3666
V <sub>62</sub> ,p.u	1.0005	1.0562	V <sub>116</sub> ,p.u	0.9996	1.0270	CPU,s	838.13	1121.17

Table X Simulation results for case D1 and D 2

Variable	CaseD1 (SBDE)	CaseD2 (SBDE)
	Generator Voltage	
V <sub>1</sub> ,p.u	1.0185	1.0011
V <sub>4</sub> ,p.u	1.0195	1.0062
V <sub>6</sub> ,p.u	1.0294	1.0078
V <sub>8</sub> ,p.u	1.0421	0.9865
V <sub>10</sub> ,p.u	1.0338	0.9963
V <sub>12</sub> ,p.u	1.0203	1.0102
V <sub>15</sub> ,p.u	0.9933	1.0071
V <sub>18</sub> ,p.u	0.9986	0.9851
V <sub>19</sub> ,p.u	0.9861	1.0109
V <sub>24</sub> ,p.u	1.0169	1.0141
V <sub>32</sub> ,p.u	0.9971	0.9992
V <sub>34</sub> ,p.u	0.9923	0.9985
V <sub>36</sub> ,p.u	0.9875	1.0019
V <sub>40</sub> ,p.u	0.9953	1.0144
V <sub>42</sub> ,p.u	0.9942	1.0108
V <sub>46</sub> ,p.u	0.9879	1.0451
V <sub>49</sub> ,p.u	1.0206	1.0223
V <sub>54</sub> ,p.u	0.9737	1.0296
V <sub>55</sub> ,p.u	0.9756	1.0156
V <sub>56</sub> ,p.u	0.9731	1.0203
V <sub>66</sub> ,p.u	1.0318	1.0222
V <sub>69</sub> ,p.u	1.0598	1.0505
V <sub>70</sub> ,p.u	1.0140	0.9967
V <sub>72</sub> ,p.u	1.0079	1.0058
V <sub>73</sub> ,p.u	0.9968	1.0050
V <sub>74</sub> ,p.u	1.0074	1.0201
V <sub>76</sub> ,p.u	0.9848	1.0084
V <sub>77</sub> ,p.u	1.0061	1.0055
V <sub>80</sub> ,p.u	1.0249	1.0315
V <sub>85</sub> ,p.u	1.0229	1.0092
V <sub>25</sub> ,p.u	1.0126	1.0042
V <sub>26</sub> ,p.u	1.0533	1.0035
V <sub>27</sub> ,p.u	1.0052	1.0125
V <sub>31</sub> ,p.u	1.0134	0.9917
V <sub>59</sub> ,p.u	1.0049	1.0335
V <sub>61</sub> ,p.u	1.0012	1.0086

V <sub>62</sub> ,p.u	0.9867	0.9950
V <sub>65</sub> ,p.u	1.0560	0.9910
V <sub>87</sub> ,p.u	1.0323	1.0312
$V_{89}$ , $p.u$	1.0548	1.0228
V <sub>90</sub> ,p.u	1.0297	0.9858
V <sub>91</sub> ,p.u	1.0193	1.0042
V <sub>92</sub> ,p.u	1.0202	1.0154
V <sub>99</sub> ,p.u	1.0089	1.0154
V <sub>100</sub> ,p.u	1.0168	1.0184
V <sub>103</sub> ,p.u	1.0138	0.9990
V <sub>104</sub> ,p.u	1.0238	1.0054
V <sub>105</sub> ,p.u	1.0122	1.0007
V <sub>107</sub> ,p.u	0.9956	1.0595
V <sub>110</sub> ,p.u	1.0102	1.0049
V <sub>111</sub> ,p.u	0.9900	1.0121
V <sub>112</sub> ,p.u	0.9960	0.9798
V <sub>113</sub> ,p.u	1.0076	1.0128
V <sub>116</sub> ,p.u	1.0551	0.9973
	Transformer Tap	
$T_8$	1.0137	0.9520
T <sub>32</sub>	1.0229	1.0053
T <sub>36</sub>	1.0002	1.0233
T <sub>51</sub>	1.0777	1.0176
T <sub>93</sub>	1.0453	0.9520
T <sub>95</sub>	1.0327	1.0518
$T_{102}$	0.9687	0.9787
T <sub>107</sub>	0.9008	1.0083
T <sub>117</sub>	0.9949	0.9561
	Capacitor banks	
Q <sub>C-5</sub> ,p.u	6.8727	6.9909
Q <sub>C-34</sub> ,p.u	8.3476	8.6539
Q <sub>C-37</sub> ,p.u	7.2743	7.5771
Q <sub>C-44</sub> ,p.u	7.8486	8.2375
Q <sub>C-45</sub> ,p.u	6.9064	7.4200
Q <sub>C-46</sub> ,p.u	6.3055	6.4317
Q <sub>C-48</sub> ,p.u	6.1935	7.6498
Q <sub>C-74</sub> ,p.u	8.8791	6.7949
Q <sub>C-79</sub> ,p.u	8.9278	8.4426
Q <sub>C-82</sub> ,p.u	6.7530	9.1108
Q <sub>C-83</sub> .p.u	6.7879	7.7867
Q <sub>C-105</sub> ,p.u	8.0907	7.2426
Q <sub>C-107</sub> ,p.u	7.6151	7.5487
Q <sub>C-110</sub> ,p.u	9.0950	7.3381
P <sub>loss</sub> ,MW	310.98	160.77
TVD,p.u	1.1966	1.0239
CPU,s	877.02	853.56
- *-		

## 6.3.2 Case D2: Minimization Of Total Voltage Deviations(TVD)

The results obtained from the proposed SBDE method for optimal settings of the control variables are given in the of Table X. The total voltage deviations are decreased from base case value of 1.7209 to **1.0239** with stressed condition. The convergence characteristic is shown in Fig.9.

#### Conclusion

In this paper, a novel Self-Balanced Differential Evolution algorithm for solving the reactive power dispatch problem is proposed. The new method makes the parameters F and C of DE become self-adaptive based on the previous fitness value. Two different objective functions such as minimization of real power loss (P<sub>Loss</sub>) and minimization of total voltage deviation (TVD) were considered under normal and stressed conditions. The proposed approach has been evaluated on the standard IEEE 57 and IEEE 118 bus test

systems under different cases. The results were compared with the results reported in the literature. The comparison confirms the effectiveness and the solution quality of the proposed approach. SBDE is superior in performance for larger power systems like IEEE 57 and IEEE 118 is proven by the shown results. It is also suitable for solving multi objective problems.

#### REFERENCES

- 1.Momoh JA, El-Hawary ME, Adapa R. A review of selected optimal power flowliterature to 1993 part I & II. IEEE TransPowerSyst 1999;14(1):96–111.
- 2. Granville S. Optimal reactive dispatch through interior point methods. IEEE Trans Power Syst 1994;9(1):136–46. 3.Quintana VH, Santos-Nieto M. Reactive power-dispatch by Successivequadratic programming. IEEE Trans Energy Convers 1989;4(3):425–35.

- 4. R. Storn and K. Price, "Differential evolution A simple and efficient adaptive scheme for global optimization overcontinuous spaces," Technical report TR-95-012, ICSI, March 1995.
- 5. Durairaj S, Devaraj D, Kannan PS. Genetic algorithm applications to optimalreactive power dispatch with voltage stability enhancement. IE (I) J-EL2006;87:42–7.
- 6. B. Zhao, C.X. Guo, and Y.J. Cao, "An Improved Particle Swarm Optimization Algorithm for Optimal Reactive

Power Dispatch," in proceedings of the Power Engineering Society General Meeting, IEEE, vol. 1, pp. 272-279, June 2005.

- 7. K. Lenin and M. R. Mohan, "Ant Colony search algorithm for optimal reactive power dispatch," Serbian journal of electrical engineering,vol.3, no.1, pp. 77-78, 2006.
- 8. M. Varadarajan and K. S. Swarup, "Differential Evolutionary algorithm for optimal reactive power dispatch," Applied soft computing, vol. 30, no. 8, pp. 1549-1561, 2008.
- 9. Wu QH, Ma JT. Power system optimal reactive power Dispatch using evolutionary programming. IEEE Trans Power Syst 1995;10(3):1243–9.
- 10. Yong Wang, Han-Xiong Li, Tingwen Huang and Long Li, "Differential evolution based on covariance matrix learning and bimodal distribution parameter setting,"
  Applied soft computing, vol. 18, pp. 232-247, 2014.
  11. H. Sharma, J. C. Bansaland K. V. Arya, "Self-balanced
- differential evolution," Journal of Computational Science, vol. 5, no. 2, pp. 312-323, March 2014.
- 12. K. Y. Lee, Y. M. Park and J. L. Ortiz, "A united approach to optimal real and reactive power dispatch," IEEE Trans Power Apparatus System, vol. 104, no. 5, pp. 1147-1153, 1985.
- 13. Himmat Singh and L. Srivastava, "Modified Differential Evolution Algorithm for Multi Objective VAR Management," Electric Power Systems Research, vol. 55, pp. 731-740, 2014
- 14 .Bhattacharya.A, Chattopadhyay. P. k, "solution of optimal reactive power flow using biogeography based optimization," Int.J Electrical Electronic engineering, vol. 4, no. 8, pp. 568-576,2010.
- 15.Duman.S, Sonmez.Y, Guvenc.U, Yorukeren.N. Optimal reactive power dispatch using a gravitational search algorithm. IET GenerTransmDistrib2012;6(6):563-76.
  16.Binod Shaw, Mukherjee.V, Ghosal. S. P, "solution of reactive power dispatch of power system by opposition based gravitational search algorithm," Electric Power System Research, vol. 53, 2014, pp. 29-40.
- 17. Dai C, Chen W, Zhu Y, Zhang X. Seeker optimization algorithm Foroptimalreactive power dispatch. IEEE Trans Power Syst2009;24(3):1218–31.
- 18. D.Devaraj, PreethaRoselyn, "Genetic algorithm based reactive power dispatch for voltage stability improvement" Electrical Power & Energy Systems, vol. 32, pp. 1151-1156,2010.
- 19.Preetha Roselyn, D. Devaraj and S. S. Dash, "Multi Objective Differential Evolution approach for voltage stability constrained reactive power planning problem," Electrical Power & Energy Systems, vol. 59, pp. 155-165, 2014.
- Wu QH, Ma JT. Power system optimal reactive power Dispatch using evolutionary programming. IEEE Trans Power Syst 1995;10(3): 1243–9.
- 21. Yoshida H, Kawata K, Fukuyama Y, Takamura S,

NakanishiY. A particle swarmoptimization for reactive power and voltage control considering voltagesecurity assessment.

IEEE Trans Power Syst2000;15(4):1232–9.
22. Esmin AAA, Lambert-Torres G, De-Souza ACZ. A hybrid Particle swarm optimization applied to loss power minimization. IEEE Trans Power Syst2005;20(2):859–66.
23.Tripathy M, Mishra S. Bacteria foraging-based solution to optimize both realpower loss and voltage stability limit.

IEEE Trans Power Syst2007;22(1):240-8.

- 24. Mahadevan K, Kannan PS. Comprehensive learning ParticleSwarm optimization for reactive power dispatch. Appl SoftComput 2010;10:641–52.
- 25. Subbaraj P, Rajnarayanan PN. Optimal reactive power dispatch using selfadaptivereal coded genetic algorithm. Electr Power Syst Res 2009;
- 26.Ela AAAE, Abido MA, Spea SR. Differential evolution algorithm for optimalreactive power dispatch. Electric PowerSyst Res 2011;81:458–64.
- 27. The IEEE 57-bus test system. <a href="http://www.ee">http://www.ee</a>. washington.edu/research/pstca/pf57/pg\_tca57bus.htm>. 28. The IEEE 118-bus test system.<a href="http://www.ee">http://www.ee</a>. washington.edu/research/pstca/pf118/pg\_tca118bus.htm