

The Random Pulse Width Modulation Technique for VSI for Harmonic-Spectrum Spreading Noise Cancellation

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Abstract – The Power electronics switch-based voltage source inverter (VSI) based induction motor drive are budding in almost all the industries due to their controllability. The pulse width modulation (PWM) is a main coin for the VSI performance and liability to control the drive. However the PWMs are not intellectual for reducing the high frequencies spectrum noises. The PWM is responsible for give more control degree of freedom and less harmonics spectrum noises. In the paper, the random PWM (RPWM) scheme is developed for VSI connected induction motor and study on noise reduction of the line voltage. The proposed RPWM method is capable to build a gap in the line voltage spectrum at choosy frequency in human hearing range. The proposed RPWM is developed for 1 kHz to 4 kHz carrier frequency range and voltage noise harmonic spectrum is studied for both MATLAB based software simulation and low scale experimentation for RL using PIC microcontroller platform. The Analysis, simulation and experimentation validating the proposed RPWM.

Keywords: VSI, RPWM, Random SVPWM, voltage noise harmonic spectrum, Acoustic noise, three phase voltage source inverters.

1. Introduction

The voltage source inverter (VSI) based high and medium power induction motor drive are growing in almost all the industries such as shipping and automotive industry [1-2]. Similar to VSI, multilevel inverter (MLI) has given lot of interest in power electronic application [3-8] These drives are mainly focusing on their variable speed-torque characteristics and continuous operation profile. This variable speed drives also concentrating acoustic noise reductions [9]. These acoustic noise present in the voltage and current waveform due to high frequency supply current harmonics, which also causes the vibration on the drive system. When system operated in low speed range this vibration is very high and affecting drive performance. Hence the reduction of high frequency

noise is much attractive in the research community in the academic and industry. The reduction of noise on the VSI drive is mainly done through pulse width modulation (PWM) techniques. Different PWM methods are used in a mixture of ASD claims. The lower switching frequency presents the acoustic noise amid low losses and higher switching frequency amplifies the losses in the inverter, however can reduce the acoustic hitch. The noteworthy enhancement in the acoustic as well as electromagnetic noise in random PWM (RPWM) have been developed in several publications for keeping low-audible noise profile with low switching frequency disturbances simultaneously. Many research papers are published in PWM modification, which is basically altering existing PWM pattern [10]. These PWM techniques are called as RPWM. The RPWM is has developed for VSI drive to mitigate the high frequency [11]. The innovative RPWM technique to avoid whistling along with EMI noise reductions [12]. The quality of output waveforms as well as the performance can be enhanced based on the PWM theory. Recently fixed switching frequency SVPWM methods are used in three-phase inverter [12-13] in addition with harmonics eliminations. The author in [14-15] examines several brands of RPWM methods from observation of harmonic spreading and efficiency. There are two categories of RPWM: one has a fixed switching frequency and the other is based on the variable switching frequency. In RPWM based techniques, the power of noise is spread in wide choice of frequency domain which increases the voltage acoustic noise and vibration [16-18]. As a result, when RPWM is used, switching of power converters is required to be controlled in a way that the noise is reduced at desired range of frequency (resonant frequency of load).

The RPWM technique is presented in [19,20] for improving acoustic and EMI characteristics. The methods based on regulating the duration of the Null vector switching or adjusting the all three phase corresponding pulse positions switching period are introduced in [18]. The Pedersen *et al.* [21-

22]attended an RPWM varying $\pm 1\text{kHz}$ spread range. The reduced noise power spectrum in a particular interval in frequency domain by eliminate in the selective range of switching frequencies. Beside with providing a space in the frequency spectrum, this technique leads to add to in peak of power spectrum density. Along with noise reductions the VSI fed drives are required to maintains the fundamental voltage, which give a ensure the wider range of speed and power characteristics. With this aim, many researches are reported on SVPWM to improve the fundamental voltage improvement [26,26]. Authors in [27], has proposed excellent PWM methods for improving the drive performance with common mode voltage eliminations. Based on the above mentioned discussions, the variable speed drive application VSIs are in need to satisfy to provide a higher fundamental voltage with harmonic-spectrum spreading noise cancellation. Besides, PWM modification online carrier frequency adjustment possibilities in the field of digital control using by micro-controller, complex programmable logic devices, field programmable gate array (FPGA), digital signal processor (DSP), and application specific integrated circuit (ASIC) technologies. Among all RPWM techniques [25,31] with online carrier modification handling is highly possible through FPGA since it has flexibility for online programming solution and the high efficiency architecture with a high speed and, high integration density. The FPGA technology offers reprogrammable SOC environment for particular applications [32]. However the FPGA based implementation demands high which is not desirable. Though microcontroller is not better candidate for wide range noise spectrum cancellation in on line carrier frequency injection/ adjustments. However, with respect to particular spread THD noise can be eliminated 8 bit PIC microcontroller is a preminent entrant.

The paper proposes the PWM with merging of RPWM with space vector PWM. In the proposed PWM the carrier frequency (f_c) is sampled and added and subtracted with switching frequency. The carrier frequency, f_c are altered by using f_c adjustment along with added, and subtracted fashion. The 8-bit microcontroller is used for implementing the proposed PWM. The simulation and low cost experimentation is proving the pros of the proposed PWM.

2. REVIEW OF THE CONVENTIONAL TWO-LEVEL VOLATGE SOURCE INVERTER AND RANDOM PWM

The Fig.1 illustrates the three-phase two-level voltage source inverter associated variable speed induction motor drive system. Here, the pole voltage are

associates symmetrical phases with 120-degree phase different namely U, V, W. The Inverter contains of six semiconductor switches (T_1 to T_6) with 180-degree phase shift continuous conduction. The upper and lower switch has 180 phase shift and the inverter switch separate with 60-degree interval operation each. In every 60-degree any one of the upper and any two lowers, or two upper with one lower switch are tuned ON and/or turned OFF for providing symmetry operation. Hence, the for one cyclic operation for the inverter has eight possible ON and OFF switching combination (in that six of them is consider as active switching and two are called zero switching). The six active switches are [001], [010], [011], [100], [101], [110] which are producing the fundamental voltage for the inverter. Similarly, the zero switches [111], [000] are producing the zero-output voltage on the inverter, which are called as zero switching or commutation switching.

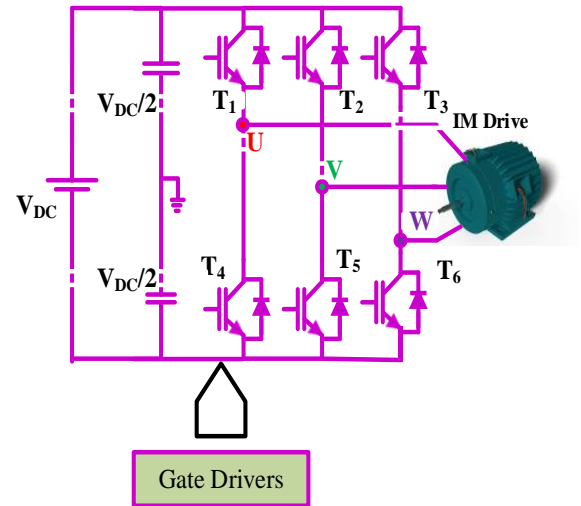


Fig.1. Three Phase Inverter fed Induction Motor

The zero switching states are used for providing circuit commutation which ensures dc-link balancing. The inverter volt-sec balancing is key factor for maintain the better harmonics voltage and current profile. The volt-sec balancing is derived from the below Eq (1),

$$\int_0^{T_c} V^* = \int_0^{T_a} V_a dt + \int_{T_a}^{T_a+T_b} V_b dt + \int_{T_a+T_b}^{T_c} V_c dt \quad (1)$$

$$V^*\{T_c\} = V_a\{T_a\} + V_b\{T_b\} + V_c\{T_c\} - T_a - T_b \quad (2)$$

$$T_a = \frac{\sqrt{3}T_s V^*}{V_{DC}} \sin\left(\frac{\pi}{3} - \theta\right) \quad (3)$$

$$T_b = \frac{\sqrt{3}T_s V^*}{V_{DC}} \sin(\theta), 0 \leq \theta \leq \frac{\pi}{3} \quad (4)$$

$$T_s = T_c - (T_a + T_b) \quad (5)$$

Where, ($T_s = 1/f_s$) is a switching time, T_1 and T_2 is the on-time, T_0 is off time (commutation time)

Phase to Phase Voltage in Fourier

$$V_{ab} = a_0/2 + \sum_{n=1}^{\infty} (a_n \cos(n\omega t) + b_n \sin(n\omega t)) \quad (7)$$

The V_{ab} is voltage between Phase “a” and Phase “b”.

$$b_n = \frac{4V_s}{n\pi} \sin\left(\frac{n\pi}{2}\right) \sin\left(\frac{n\pi}{3}\right) \quad (8)$$

Due to the quarter wave symmetry along the α -axis, both a_0 and a_n are zero. Assuming Symmetry along the β -axis at $\omega t = \pi/6$ (60-degree) , hence the three phase output voltage can be written as,

Phase to Phase Voltage in Three Phase inverter

$$V_{ab} = \sum_{n=1,3,5}^{\infty} \frac{4V_s}{n\pi} \sin\left(\frac{n\pi}{3}\right) \sin\left(\omega t + \frac{\pi}{6}\right) \quad (9)$$

$$V_{bc} = \sum_{n=1,3,5}^{\infty} \frac{4V_s}{n\pi} \sin\left(\frac{n\pi}{3}\right) \sin\left(\omega t - \frac{\pi}{2}\right) \quad (10)$$

$$V_{ca} = \sum_{n=1,3,5}^{\infty} \frac{4V_s}{n\pi} \sin\left(\frac{n\pi}{3}\right) \sin\left(\omega t - \frac{7\pi}{6}\right) \quad (11)$$

Table 1. VSI switching vector, phase voltage and line voltage.

Mode	V^*	Line to Line voltage			Switching vector		
		V_{UV}	V_{VW}	V_{WU}	U	V	W
1	V_0	0	0	0	0	0	0
2	V_1	1	0	0	1	0	0
3	V_2	0	1	-1	1	1	0
4	V_3	-1	1	0	0	1	0
5	V_4	-1	0	1	0	1	1
6	V_5	0	-1	1	0	0	1
7	V_6	1	-1	0	1	0	1
8	V_7	0	0	0	1	1	1

To control the VSI, numerous modulation approaches were reported in literature [Br]. In which sinusoidal PWM (SPWM) and SVPWM are the commonly used PWM techniques [18, 19]. were developed in RPWM approaches which can reduce the EMI and lower order harmonics. The Fig .2 show the two-level voltage source inverter space vector diagram. Where the V^* is represented as resultant voltage. The active vector switches are placed in

every edge of the space vector hexagonal and the zero vector switches are placed in the origin ‘O’. The Fig.3 shows the active and zero vector switching positions.

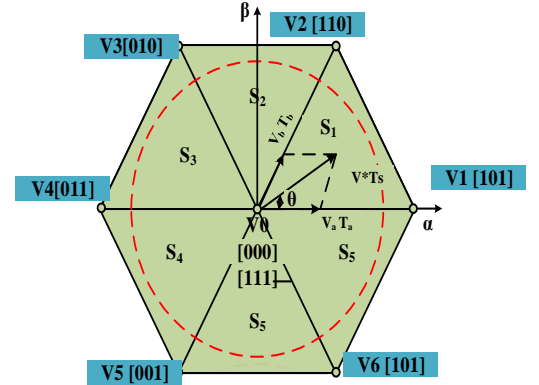


Fig.2. Space vector diagram (SVD) and switching

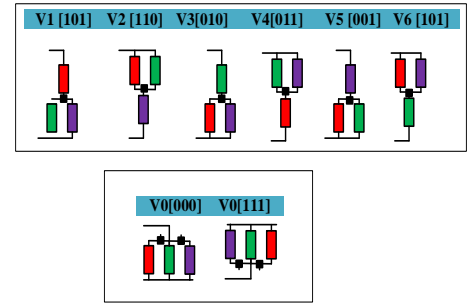


Fig.3. Space vector diagram (SVD) and switching

In SVPWM, the reference vector, V^* is sampled with a switching frequency f_s ($T_s = 1/f_s$). The V^* generated from alpha -beta transformation from three phase references. The switching vector diagram is with their switching events are shown in Fig.3, which are consist of six-sector and each sector is created using three switching states (combination of zero and non-zero vectors). Based on the zero vectors positioning in the switching vector sequence the continuous and discontinuous mode is selected in the SVPWM strategy. These selections decisive for reducing harmonic substance and the switching losses. Here the reference is generated by using on-time equations of the SVD. Then the symmetrical carrier is compared with reference signal. The SPWM and SVPWM is similar way of approach. In SPWM, the three-phase reference signal directly compared with carrier signal, where as in SVPWM composed time manner and finally compared with carrier signal. Though SPWM and SVPWM is a frequently used method for all VSI applications. These methods had discrete frequency components in their current spectrum which cause the EMI and acoustic noise in the induction motor. To

distribute the discrete components from the current spectrum of the motor is called as RPWM.

3. Noise Investigation

When the induction motor is operated in non-sinusoidal power supply (quasi-square wave form) the acoustic noise is created on the starter. This may excite the system resonant frequencies which increases the acoustic noise and vibration [peryl3-15]. For acoustic noise reduction, a weighted IEC 61672-2013-standard range of RPWM method compared to conventional RPWM technique is to reduce broad band noise by 2-6 dB over the full modulation index range. This range produces a better acoustic noise. Acoustic noise generated by electrical motors driven by a pulse width modulated power electronic inverter. Various PWM techniques (i.e. SPWM, RPWM, FCF-RPWM, RCF-RPWM, and SVPWM) are used to reduce the greatest annoyance of the motor. The proposed method of RSPVPM technique used to reduce the acoustic noise below 10 dB. The human ear is the remarkable acoustic system. The ear is capable of responding to sounds over a frequency range from about 16-20Hz up to frequencies in the 16-20 kHz range. Above 20 kHz is the greatest annoyance. The acoustic noise creates an unpleasant atmosphere to work and the mechanical vibration causes gap separation between the stator and rotor. The best way to reduce audible noise radiated from the AC motor is to increase the PWM switching frequency up to 18 kHz. A randomized pulse position method in which, the discrete harmonics are significantly reduced and harmonic power spread over as a continuous spectrum. The discrete harmonic spectra occur at switching frequency and its multiples. The normal voltage source inverter produces the noise shown in Fig.3; it was analyzed by spectrum scope. The acoustic noise produced above 20 dB for the three-phase voltage source PWM inverter. Fig. 4 and Fig. 5 shows the spectrum of noise in three phase VSI.

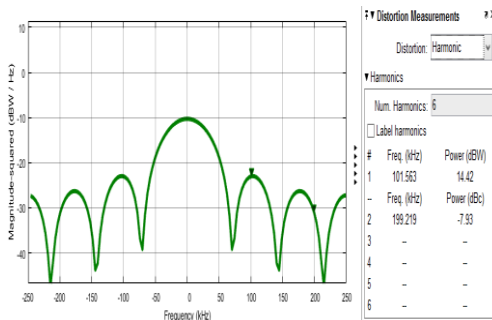


Fig.4. Spectrum of VSI line voltage

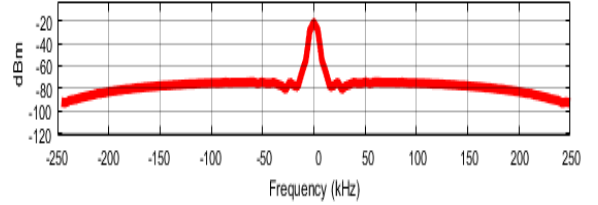


Fig.5. Power noise in dB

3. Proposed Random Space Vector PWM Technique

As mentioned in the introduction PRWM has developed using binary logic circuit using flip-flop and comparators. The RPWM for noise reduction has been evaluated when the switching frequency is selected randomly. In this way, first in each cycle the switching period is selected from the proper range, then according to time percentage of da , db , and $d0$, the switching pulses has been generated.

As shown in Fig. 6, the randomised triangular carrier generation is developed in the proposed RPWM using two fixed carrier ' f_c+ ' and ' f_c- '. Here the ' f_c+ ' is non-inverting carrier signal and ' f_c- ' is an inverting one. The PRPS based shift register has two XOR and one OR gate. The proposed method used 8-bit shift register, where the bits are denoted as b_1 to b_8 . In order create the more randomness the bit b_4 and b_5 is connected with one XOR gate and the bit, b_6 and b_8 is connected with other XOR gate. These XOR gate outputs are connected with OR gate and give the output and entire bit to the shift register.

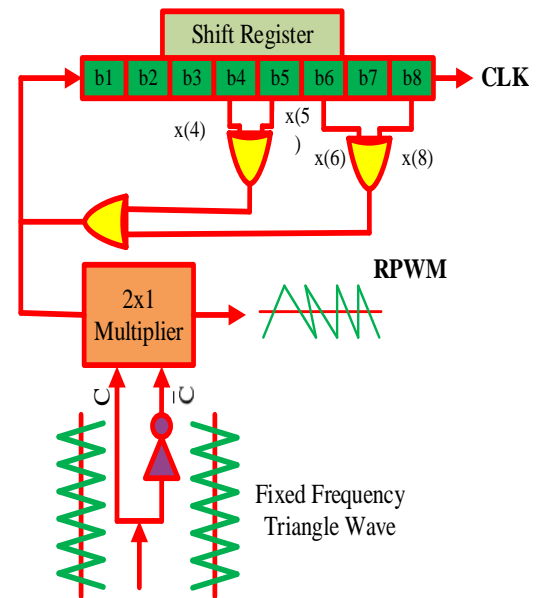


Fig.6. RSPVPM signal generator

All of the register elements share a common clock input, which is omitted from the symbol for reasons of clarity. The data input to the LFSR is generated by XOR or XNOR the tap bits; the remaining bits function as a standard shift register. The sequence of values generated by an LFSR is determined by its feedback function (XOR against XNOR) and tap selection. For example, consider two 2-bit XOR based LFSRs with different tap selections (Fig.6). Based on the OR-gate output the multiplier receiving signal from either from ' f_c+ ' or ' f_c- '. The correspondence switching states selection is chosen based on the pulse pattern output.

4. Simulation and Results

The proposed RPWM is modeled with six switch voltage source inverter with 0.75kW induction motor using MATLAB/Simulink platform. The table2 illustrates the parameters of simulation for inverter and induction motor.

Table 2. Simulation parameters

Parameters	values
Power (P)	1 KW
Line to Line voltage (V_L)	400 V
Frequency (f)	50 Hz
Stator resistance (R_s)	1.4 Ω
Stator inductance (L_s)	0.00587 H
Rotor resistance (R_r)	1.35 Ω
Speed	1400 rpm
I_{rms}	3 A
V_{rms}	400V
Torque(T)	5Nm

The highest randomization freedoms, nonlinearities components, dead-time and filters have been ignored in the simulation. The simulation study is developed for the PWM switching frequency in tuned with 1 kHz to 25 kHz frequency range. The VSI line voltage (V_L) with high modulation index, $M_a = 0.9$. Now, when the VSI functioned at 0.9 M_a , the voltage is measured as 270V. Fig.8 illustrates the THD spectrum for line -voltage, where the percentage line-voltage THD is observed as 10.16% for $M_a = 0.9$.

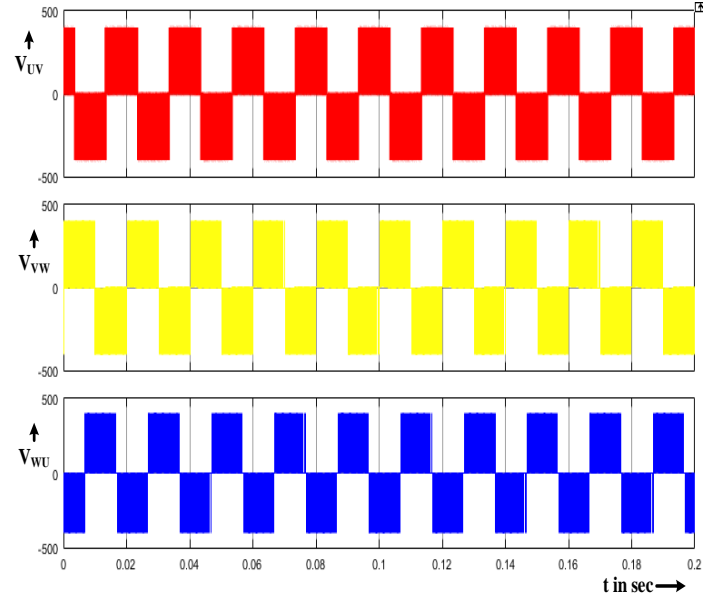


Fig. 7 RSVPM VSI line voltage, $M_a=0.9$.

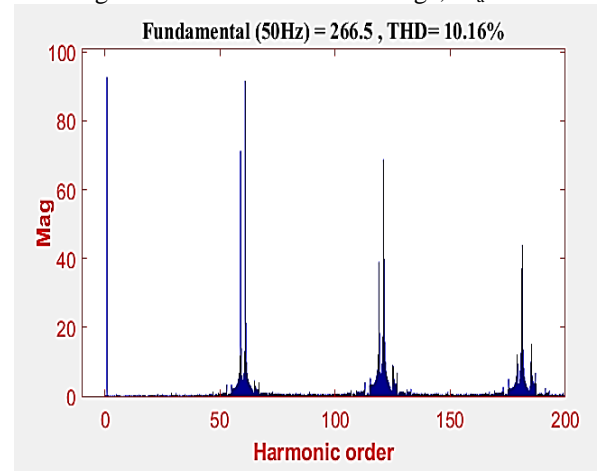
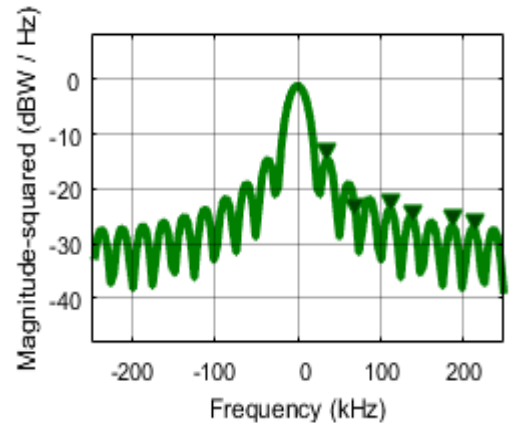
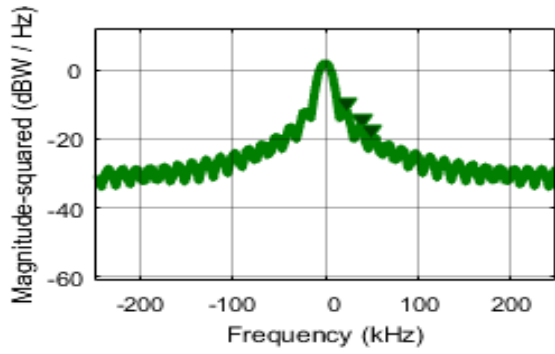


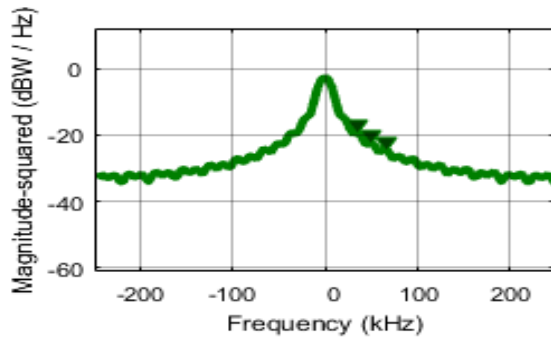
Fig. 8 Harmonics spectrum of line voltage, $M_a=0.9$



(a)

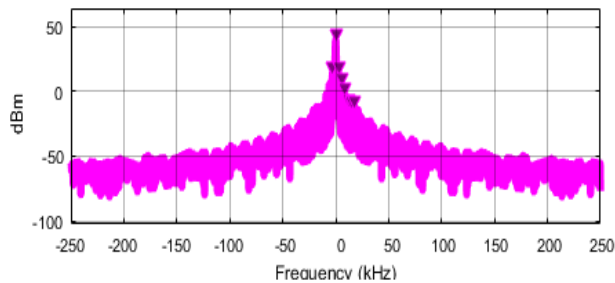


(b)

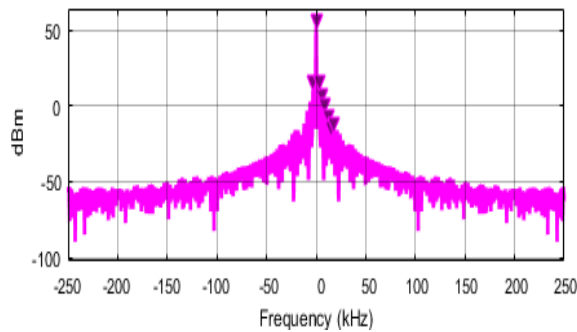


(c)

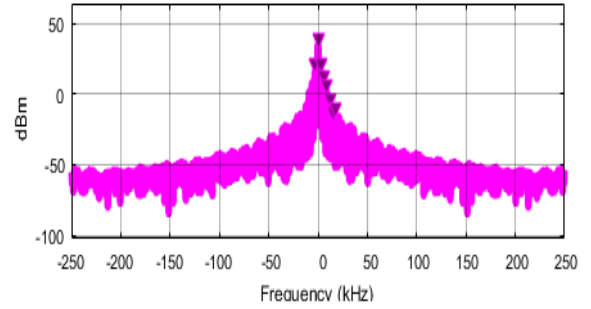
Fig. 9. Simulation results of the motor voltage spectrum for modulation index 0.5, 0.7 and 0.9 for 4kHz.



(a)



(b)



(c)

Fig. 10. Simulation results of the motor voltage spectrum for modulation index 0.5, 0.7 and 0.9 for 4kHz.

The Fig.9 and Fig.10 shows the voltage spectrum for VSI functioned at lower for modulation index 0.5, 0.7 and 0.9 for 4kHz. Here, when the inverter operating $M_a = 0.5$, the noise is measured as 22.14 dB. However, the, when inverter operating at $M_a = 0.9$, for the same switching frequency range, voltage noise is measured as 16.29 dB. From the results, when lower modulation ranges the voltage waveform had higher noise against higher M_a .

5. Experimental Results

For the investigation of the experimental verification for the proposed RPWM, the 200W show six switch VSI is designed and collaborated with PIC microcontroller digital implementation platform.



Fig.11.shows the experimental setup of the three-phase VSI connected RL load

The RPWM is developed in assembly code and implemented in the 5 kHz switching frequency with 5 microsec dead time. Fig.11.shows the experimental setup of the three-phase VSI connected RL load. The 1000microF capacitor and 10 ohm, 4 mH RL load used for the DC-link and load respectively. The TLP250 gate driver circuit is used for six MOSFETs. The voltage and THD waveforms are measured using 2 channel DSO. The inverter is having a degree of freedom to change their modulation index.

The Fig.12 shows the gating pulses of inverter switch T1 to T2 , Fig.13 shows the gating pulses of inverter switch T3 to T4, and Fig.14 shows the gating pulses of inverter switch T5 to T6. The dead time of the same inverter leg switch is shown in fig.15. At first the test was performed between 5kHz lower modulation index ($M_a = 0.5$) and the inverter tested for higher modulation index ($M_a = 0.9$). The output line voltage of VSI for 4kHz is shown in Fig.16. Here, the line voltage of the inverter is measured as 60V. In this case the noise is calculated as 9.8 dB and it is rising slightly when the switching frequency rising to 11 dB for 6kHz, f_s . In similar way, when inverter is operates at higher M_a 0.9, the output line voltage of VSI for 4kHz is shown in Fig.17. Here, the line voltage of the inverter is measured as 120V. In this case the noise is calculated as 14.8 dB and it is rising slightly when the switching frequency rising to 9 dB for 4kHz. The fig.44 shows the line voltage THD spectra for $M_a = 0.9$. From the results, the THD is measured as lesser values as

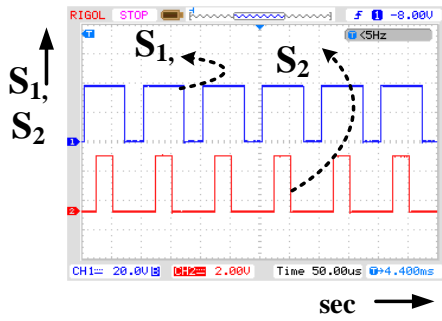


Fig.12. gating pulses of inverter switch S_1 to S_2

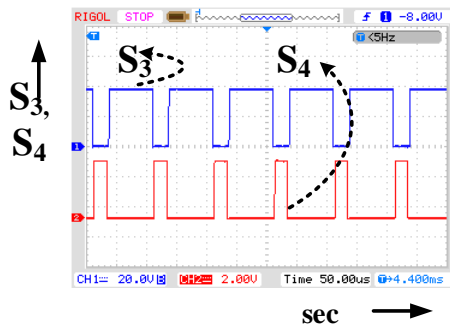


Fig.13. gating pulses of inverter switch S_3 to S_4

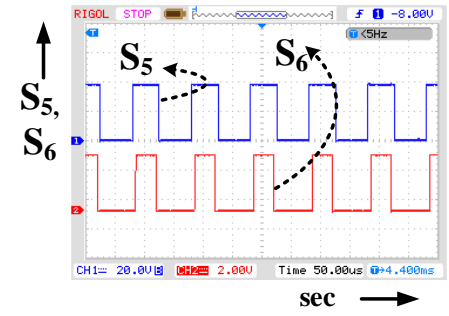


Fig.14. gating pulses of inverter switch S_5 to S_6

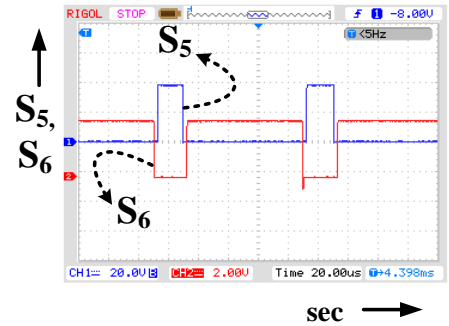


Fig.15. gating pulses of inverter switch S_2 to S_3

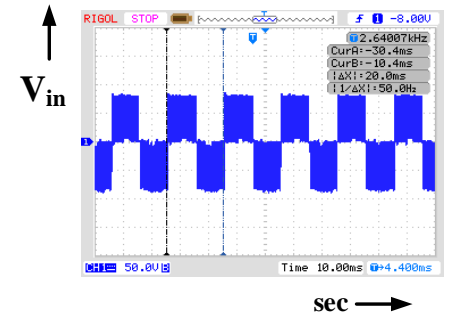


Fig.16. Experimental Line voltage for 0.5 M_a

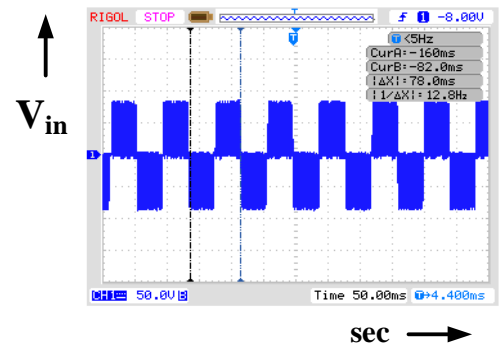


Fig.17. Experimental Line voltage for 0.9 M_a

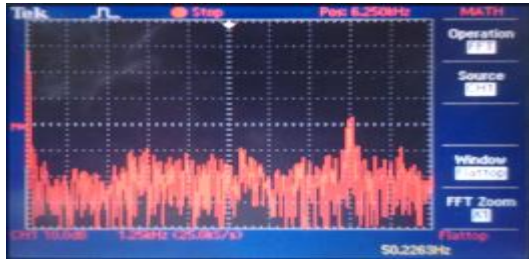


Fig.18. Experimental Line voltage noise for 0.5 M_a

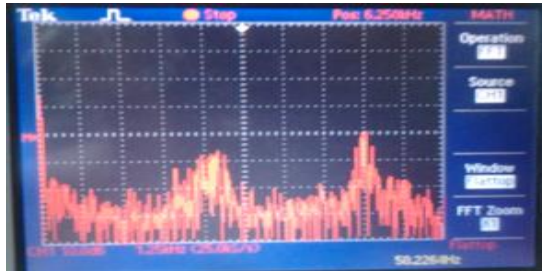


Fig.19. Experimental Line voltage noise for 0.9 M_a

6. Conclusion

The proposed RPWM method used inverter for spreading the harmonic noise cluster can excite the system resonant frequencies and reduced the acoustic noise in line voltage. The proposed Random pulse width modulation has well maintained and has more control degree of freedom and less harmonics spectrum noises. The proposed RPWM method is capable to build a gap in the line voltage spectrum at choosy frequency in human hearing range. The proposed RPWM is developed for 1 kHz to 4 kHz carrier frequency range and voltage noise spectra is studied for both MATLAB based software simulation and low scale experimentation for RL using PIC microcontroller platform. The Analysis, simulation and experimentation validating the proposed RPWM.

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